# Numerical Calculation of Transient Thermal Characteristics in Gas-Insulated Transmission Lines

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## Abstrak

Guna kajian mendalam karakteristik termal pada jalur transmisi gas terisolasi (gas-insulated transmission lines, GILs) terpasang di atas tanah, model elemen-hingga medan cairan kopling dan medan panas didirikan, di mana asumsi yang sesuai dan kondisi batas yang diberikan. Proses kenaikan suhu transien GIL pada kondisi suhu lingkungan variabel, kecepatan angin dan radiasi matahari diinvestigasi. Kondisi ekuivalensi koefisien perpindahan panas konvektif permukaan dan kondisi batas fluks panas diperbarui dalam proses analisis. Berbeda dengan metode elemen hingga (finite element method, FEM) tradisional, pada penelitian ini variabilitas sifat termal terhadap suhu dipertimbangkan. Hasil perhitungan divalidasi oleh hasil tes penelitian lain. Simpulan memberikan metode dan dasar teori untuk kajian mendalam karakteristik kenaikan suhu transien GILs di lingkungan terbuka.

*Kata kunci*: fluks panas, kenaikan suhu transien, koefisien transfer panas konvektif, lingkungan terbuka, model elemen-hingga

## Abstract

For further knowledge of the thermal characteristics in gas-insulated transmission lines (GILs) installed above ground, a finite-element model of coupling fluid field and thermal field is established, in which the corresponding assumptions and boundary conditions are given. Transient temperature rise processes of the GIL under the conditions of variable ambient temperature, wind velocity and solar radiation are respectively investigated. Equivalent of surface convective heat transfer coefficient and heat flux boundary conditions are updated in the analysis process. Unlike the traditional finite element method (FEM), the variability of the thermal properties with temperature is considered. The calculation results are validated by the tests results reported in the literature. The conclusion provides method and theory basis for the knowledge of transient temperature rise characteristics of GILs in open environment.

*Keywords*: convective heat transfer coefficient, finite element model, heat flux, open environment, transient temperature rise

## 1. Introduction

The trend of increasing power consumption needs higher electrical energy to be transported from the power plants to load centers. Construction of more overhead lines and pole towers is not suitable for environmental protection especially in metropolitan areas. Gasinsulated transmission lines (GILs) represent a new technology for high power transmission instead of traditional overhead lines and cables, with the advantages such as space saving, high transmission capability and low energy loss [1-6].

Knowledge of the temperature profiles of GILs is critical important in understanding the improvement of the design and manufacture processes in order to keep the operation temperature at safety levels. Analytical methods in conjunction with empirical approximations have been used to analyze the thermal characteristics of the GILs [7, 8]. However, these methods are incapable of obtaining the temperature distribution and not sufficient for transient thermal calculation. Therefore, in order to predict the temperature profile of GIL as reliably as possible, one must resort to numerical calculation. Finite element methods (FEM) have been most widely used in the thermal analysis of power apparatus. The literature [9] used FEM to solve the coupled electromagnetic and thermal problems in GILs installed inside a tunnel. The literature [10] carried out a long term test and used FEM to study the unsteady state behavior of buried GILs. Based on the theory of computational fluid dynamics (CFD), the literature [11] used

FEM to investigate the thermal problem of turbulent natural convection in a 400kV GIL. However, in addition to temperature dependent physical parameters such as gas density, dynamic viscosity and thermal conductivity, the complex environmental factors are not contemplated in these models. For the operating GILs, especially the GILs installed above ground, the temperature rise will be greatly influenced by the ambient temperature, wind velocity and solar radiation. In order to study the heat transfer characteristics of the GILs comprehensively, it is necessary to analyze the temperature variation of the GILs under different environments.

In this paper, the coupled fluid and thermal finite element model is established. Heat transfer of conduction, convection and radiation in the GIL are considered. The temperature dependent heat transfer coefficients on the enclosure surface, electrical and thermal properties of the materials are updated in the iterative procedure. Wind and solar radiation are equivalent to convective boundary condition and heat flux boundary condition, respectively. Temperature rise characteristics of the GIL under time varying ambient temperature, wind velocity and solar radiation are analyzed with the proposed model. The predicted temperatures are validated against test results reported in the literature.

## 2. Solution Region and Basic Assumptions

GIL is mainly composed of aluminum enclosure, conductor, epoxy resin insulators, particle trap and insulating gas (SF<sub>6</sub>). The structure is deemed symmetrical. In order to reduce the computation cost without the loss of accuracy, a two-dimensional (2-D) model is employed in the solution procedure, as shown in figure 1. The analysis presented in this paper is based on the following assumptions:

- The GIL is infinitely long.
- Radiation effect of the SF<sub>6</sub> gas is disregarded.
- The density, viscosity and conductivity of the SF<sub>6</sub> gas and air are temperature dependent, while the specific heat is considered as constant.
- Heat transfer coefficient on the enclosure surface is temperature dependent.
- Contacts, insulators and particle traps, which have little influence on the temperature distribution of the whole GIL, are excluded in the solution region.



Figure 1 Solution region of the thermal field

## 3. Thermal Analysis

In the thermal analysis of GIL, the heat transfer mechanisms are conduction, convection and radiation. The heat generated in the conductor and the enclosure is transferred from the interior surface to the external surface by conduction. There are two convection types in the model, natural and forced convection. Natural convective heat transfer, which is caused by the density difference of the fluid, exists at the interface of the  $SF_6$  gas and the conductor and that of the  $SF_6$  gas and the enclosure. Forced convection is deemed to happen on the outer surface of the enclosure when the GIL is exposed to wind. Thermal radiation heat transfer from the enclosure surface to the surrounding air and between the conductor and the enclosure is significant, especially when the temperature difference increases. To the authors' knowledge, approximately 60% of the heat generated in the GIL is dissipated to the surrounding air by radiation.

Applying the finite element technique, the whole solution region of the GIL is divided into many elements. The material properties and the governing equations are considered over all the elements and expressed in terms of unknowns at the nodes. The Galerkin finite element procedure is applied, resulting in a set of simultaneous equations, the solution of which gives approximation of the unknowns. Moreover, appropriate boundary and initial conditions are needed in the thermal analysis of GIL. The boundary conditions specify the thermal conditions at the boundary of solution region and the fluid-solid interface, and the initial condition specifies the temperature distribution of the GIL at the initial time(t=0) of transient analysis.

## 3.1. Governing equations

The thermal load is a function of time when studying the variation of the temperature rise. Therefore, time terms are included in the equations of heat transfer in the GIL. The differential equation governing the heat conduction in the conductor and enclosure is described as

$$\lambda_{\rm s} \nabla^2 T + Q = \rho_{\rm s} C \frac{\partial T}{\partial t} \tag{1}$$

where  $\lambda_s$ ,  $\rho_s$  and *C* are, respectively, the thermal conductivity, density, specific heat and of the conductor or the enclosure, *Q* is volumetric heat source, *T* is the Kelvin temperature and *t* is the time.

The following set of nonlinear equations is solved simultaneously with FEM: The continuity equation [12, 13]

$$\frac{\partial \rho_{\rm f}}{\partial t} + \rho_{\rm f} \nabla \cdot \boldsymbol{V} = 0 \tag{2}$$

the Navier-Stokes equation

$$\rho_{\rm f}\left(\frac{\partial \boldsymbol{V}}{\partial t} + \boldsymbol{V} \cdot \nabla \boldsymbol{V}\right) = \mu_{\rm f} \nabla^2 \boldsymbol{V} + \rho_{\rm f} g \cdot \nabla P \tag{3}$$

and the energy equation

$$\rho_{\rm f} C_p \left( \frac{\partial T}{\partial t} + \boldsymbol{V} \cdot \nabla T \right) = \lambda_{\rm f} \nabla^2 T \tag{4}$$

where  $\rho_{\rm f}$  is the gas density, **V** is the gas velocity,  $\mu_{\rm f}$  is the dynamic viscosity, *g* is the gravity acceleration, *P* is the pressure, and  $C_{\rho}$  is the specific heat.

Numerical calculation of the thermal characteristics in the GIL will be more accurate, provided the material properties including the gas density, thermal conductivity and dynamic viscosity are considered temperature dependent. The density of the SF<sub>6</sub> gas is given by

$$\rho_{\rm f}(T) = \rho_0 P C_1 / (T C_2) \tag{5}$$

The thermal conductivity and dynamic viscosity of the SF<sub>6</sub> gas are calculated with the Sutherland's law [14]:

$$\lambda_{\rm f}(T) = \lambda_0 (T / C_1)^{1.5} (C_1 + C_2) / (T + C_2)$$
(6)

$$\mu_{\rm f}(T) = \mu_0 (T/C_1)^{1.5} (C_1 + C_2) / (T + C_2) \tag{7}$$

where  $\lambda_0$ ,  $\rho_0$  and  $\mu_0$  are, respectively, the gas density, thermal conductivity and dynamic viscosity at room temperature,  $C_1$  and  $C_2$  are constants.

# 3.2. Heat Source Evaluation

Power losses generated in the conductor and the enclosure of the GIL is calculated with finite element procedure introducing magnetic vector potential. The power loss per unit length in

the conductor or the enclosure, which is used as the volumetric heat source for the thermal analysis, is calculated as follows:

$$Q = \sum_{i=1}^{N} q_i = \sum_{i=1}^{N} \frac{\boldsymbol{J}_i \boldsymbol{J}_i^*}{\sigma_i}$$
(8)

where *N* is the element number,  $q_i$ ,  $J_i$  and  $\sigma_i$  are the power loss, total current density and conductivity of the *i* th element, respectively.

#### 3.3. Convective Heat Transfer Boundary

The convective heat transfer boundary condition on  $S_2$  does not need to be specified particularly, because the convective heat transfer is calculated with CFD in the iterative procedure. The convective heat transfer boundary condition on  $S_1$  is described by considering an energy balance at the surface stated as

$$-\lambda_{\rm s}\left(\frac{dT}{dx} + \frac{dT}{dy}\right) = h(T - T_a) \tag{9}$$

where h is the convective heat transfer coefficient,  $T_a$  is the temperature of the surrounding air.

Great efforts have been made to determine the convective heat transfer coefficient on the outer surface of enclosure, because it is correlated with many factors, such as gas velocity, temperature, and characteristic size. With regard to the GIL installed above ground, the heat transfer will be greatly affected by the wind. The heat transfer coefficient is composed of the natural convection part and the forced convection part caused by wind as follows

$$h = h_{\rm n} + h_{\rm f} \tag{10}$$

where  $h_n$  and  $h_f$  are, respectively, the natural and forced convective heat transfer coefficient.

The natural convective heat transfer coefficient can be determined by classical Nusselt number described as [15]

$$Nu = C(Gr \cdot Pr)^n \tag{11}$$

$$Gr = g\alpha \Delta T D_{\rm to}^3 / v^2 \tag{12}$$

$$Pr = v / a \tag{13}$$

$$h_{\rm n} = N u \cdot \lambda \,/\, D_{\rm to} \tag{14}$$

where *Nu* is the Nusselt number, *Gr* is the Grashof number, *Pr* is the Prandtl number, *C* and *n* are constants,  $\alpha$  is the coefficient of cubical expansion,  $D_{to}$  is the outer diameter of the enclosure, *v*, *a* and  $\lambda$  are, respectively, the kinetic viscosity, thermal diffusivity and thermal conductivity of the air.

The heat dissipated by forced convection is presented in (15) and the forced convective heat transfer coefficient is calculated with Newton's law of cooling which is presented in (16) [7].

$$\Phi_{\rm f} = 7.5(V \cdot D_{\rm to})^{0.6}(T - T_a) \tag{15}$$

$$h_{\rm f} = \Phi_{\rm f} / A(T - T_{\rm a}) \tag{16}$$

where *A* is the surface area of the enclosure.

#### 3.4. Heat Flux Boundary

For the GIL exposed to solar radiation, the heat flow on  $S_1$  caused by solar radiation is described as

 $\Phi_{\rm s} = \varepsilon_{\rm t} D_{\rm to} \omega \tag{17}$ 

where  $\varepsilon_t$  is the absorption factor of the solar radiation and  $\omega$  is the heat flux of solar radiation. According to Fourier's law, the average heat flux caused by solar radiation is shown as  $q = \Phi_{\rm s} / A \tag{(}$ 

Note that the convective heat transfer boundary and the heat flux boundary are not applied simultaneously. The convective heat transfer boundary is adopted when the GIL is cooled by the wind, while the heat flux boundary is adopted when there is solar radiation.

# 3.5. Radiation Heat Transfer Boundary

In addition to convection, there is radiative heat exchange between the conductor and the enclosure and between the enclosure and its surroundings. The heat transfer by radiation is found to have large effects on the temperature rise of the whole GIL. The mathematical formulation of the radiation boundary condition is obtained by [14]

$$-\lambda \frac{dT}{dx} - \lambda \frac{dT}{dy}\Big|_{\Gamma_2, \Gamma_3} = \sigma \varepsilon F_{ij} (T_i^4 - T_j^4)$$
(19)

$$F_{ij} = \frac{1}{A_i} \int_{A_j} \int_{A_j} \frac{\cos \theta_i \cos \theta_j}{\pi r^2} dA_i dA_j$$
(20)

where  $\sigma$  is Stefan-Boltzmann constant,  $\varepsilon$  is the emissivity of the surface,  $F_{ij}$  is the view factor,  $A_i$  and  $A_j$  are the element areas, r is the distance between the two elements,  $\theta_i$  and  $\theta_j$  are the polar angles formed by the radiation line and the normal of the two elements.

# 4. Model Results and Discussion

In this section, the model proposed is employed to investigate the transient thermal performance of the GIL in the cases of time varying ambient temperature, wind velocity and solar radiation, respectively. The more complex environmental condition that includes both wind velocity and solar radiation is not mentioned in this paper. The results are compared with tested data reported in [7]. The current frequency is 60 Hz, and the pressure of the SF<sub>6</sub> gas is 0.4 MPa. The dimensions and materials of the GIL are given in Table 1.

| Table. 1            | Dimensions and Materials of the GIL |           |
|---------------------|-------------------------------------|-----------|
| Item                | Conductor                           | Enclosure |
| Material            | A6063-T5                            | A6063-T5  |
| Inner diameter (mm) | 140                                 | 480       |
| Outer diameter (mm) | 180                                 | 504       |

#### 4.1. Temperature Variation of the GIL under Time Varying Ambient Temperature

Under the condition of no wind or solar radiation, the variation of GIL temperature in 10 hours at the current of 7300 A is illustrated in Figure 2. The initial temperature of the conductor and the enclosure is the same as the ambient temperature before the current is loaded. In the first 3 hours, an appreciable increase in the conductor and the enclosure is recognized. During the next 7 hours, the temperature rises slow down gradually and nearly come to a steady-state. Finally, the temperature rise of the conductor is 67 K and that of the enclosure is 34K. The temperature distributions inside the GIL at different times are illustrated in Figure 3. The maximum temperature occurs right above the conductor, while the minimum temperature at the bottom of the enclosure. The difference between the temperature distributions of the GIL after 6 hours is unobvious. The variation of the convective heat transfer coefficient on the enclosure surface is shown in Figure 4. The convective heat transfer coefficient increases rapidly in the first 2 hours and then reaches stability gradually.

# 4.2. Temperature Variation of the GIL under the Effect of Wind

The temperature variation of GIL exposed to wind for 10 hours at the current of 7300 A is illustrated in Figure 5. Before exposing to the wind, the temperature of the conductor and the enclosure are 89  $^{\circ}$ C and 56.3  $^{\circ}$ C, respectively.

(18)



Figure 2 Temperature variation of the GIL under time varying ambient temperature



Figure 3. Temperature distributions of the GIL at different times



Figure 4. Heat transfer coefficient variation under time varying ambient temperature

Within the first hour after the wind is applied, the velocity of the wind increases to 1.73 m/s gradually and the temperature of the conductor and the enclosure decreases by 0.7  $^{\circ}$ C and 3.6  $^{\circ}$ C, respectively. In the following 3 hours, the wind velocity variation is less than 1m/s, no obvious temperature fluctuation on the conductor and the enclosure is found because the heat transfer by convection and radiation almost reaches an equilibrium state. Furthermore, the temperature of the enclosure is more susceptible to the wind than the conductor. The reason lies in that the convective heat transfer capability of the air around the enclosure is directly affected by the wind which varies the proportions of the heat transfer by convection and radiation, while the heat transfer characteristics inside the GIL are nearly unaffected.



Figure 5. Temperature variation process for case of wind



Figure 6. Surface convective heat transfer coefficient variation for case of wind

Figure 6 gives the variation of the convective heat transfer coefficient on the enclosure surface. Noticeable variation is shown after exposing the GIL to the wind, and the coefficient is approximately proportional to the change of the wind velocity.

## 4.3. Temperature Variation of the GIL under the Effect of Solar Radiation

The temperature rises of the conductor and enclosure due to solar radiation after the current-induced temperature rise has leveled off are shown in Figure 7.



Figure 7 Temperature variation process in the case of solar radiation

The temperature of the GIL rises with increasing radiation flux in the range of 0-770  $W/m^2$ . Moreover, the temperature of the enclosure is a little more sensitive to solar radiation than the conductor, and the maximum temperature rise of the conductor and the enclosure are 22.2 K and 26.3 K, respectively. The influence of the solar radiation over the temperature rise is evident and deserves special consideration for better thermal design of GIL.

# 5. Conclusion

In order to investigate the transient heat transfer characteristics of the GIL installed above ground, a finite-element model is established and appropriate boundary conditions were presented. Temperature variation process of the GIL under time-varying ambient temperature, wind velocity and solar radiation are described in detail, respectively. The calculated results correspond well with the tests results reported in the literature. The following conclusions are obtained:

- The good agreement between the calculated and tested results shows that the scheme using convective heat transfer boundary and heat flux boundary, respectively, in the model under the condition of wind and solar radiation is effective.
- When the time varying ambient temperature is only considered in the model, in the first 3 hours, the GIL temperature rises rapidly and gradually comes to the steady state in the next 7 hours. The convective heat transfer coefficient on the enclosure surface is deemed to be constant after the first 2 hours.
- The temperature of the enclosure is more susceptible to wind than the conductor because the outer surface convective heat transfer coefficient of the enclosure will be affected by wind directly.
- The temperature variations of the conductor and enclosure due to solar radiation are obvious and present the same tendency although the temperature of the enclosure is slightly more sensitive to solar radiation than the conductor.

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