# Energy scavenging-aided NOMA uplink communications: performance analysis

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#### ABSTRACT

Energy scavenging-aided nonorthogonal multiple access (NOMA) networks significantly ameliorate energy-and-spectral efficiencies thanks to superimposing a multitude of user signals for concurrent transmission and harvesting radio frequency energy. Practically, energy harvesters possess non-linear characteristic and their efficiency is enhanced considerably with deployment of multiple antennas. Moreover, communication reliability and harvested energy are directly influenced by wireless propagation which induces simultaneous effects of shadowing, path loss, and fading. Accordingly, the current paper assesses analytically outage probability and throughput of energy scavenging (ES)-aided NOMA uplink communications (eNOMAu) taking into account the above-addressed realistic factors ( $\kappa - \mu$  shadowed fading, multi-antenna deployment, ES nonlinearity). The results reveal considerable performance degradation caused by ES non-linearity and wireless propagation. Additionally, desired system performance can be reached flexibly with appropriate specification selection. In addition, accreting a quantity of antennas drastically mitigates the outage probability of eNOMAu, which can be minimized with optimal ES time selection. Furthermore, the proposed eNOMAu is considerably superior to its eOMAu counterpart.

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## 1. INTRODUCTION

5G/6G systems grant a multitude of emerging wireless applications for a massive number of devices but enforce serious challenges on telecommunication infrastructure, particularly in current scenarios of spectrum and energy shortages, to supply sufficiently spectrum and energy for these devices [1], [2]. Therefore, solutions for improving energy and spectral efficiencies are essential and urgent.

Nonorthogonal multiple access (NOMA), which was recommended for 5G/6G networks, is a feasible solution to ameliorate spectral efficiency [3]. By distributing distinct power levels to diverse users, NOMA exploits efficiently successive decoding in combination with interference cancellation to further mitigate system outage. Furthermore, harvesting radio frequency energy present in wireless signals by NOMA users can be considered as a helpful solution in meliorating energy efficiency. Notably, an implementable ES circuit is deployed in 5G/6G transceivers [4]. Notwithstanding, a majority of performance analyses pertinent to ES have

characterized ES to be linear for tractability [5]. Realistically, ES circuit is implemented by nonlinear elements, namely capacitors, inductors, diodes. Thereby, characterizing energy harvesting ought to take the non-linearity of circuit elements into account. So far, various non-linear energy harvesting models have modelled such non-linearity [3], [6], [7].

Energy scavenging-aided NOMA uplink communications (eNOMAu), viz. Figure 1, enables two NOMA transmitters (U1 and U2) to concurrently send their data to the same receiver (NR) and to scavenge energy from a power source (PS) for their transmission wherein high-and-stable power television/radio broadcasting transmitters can play a role as PS. To further ameliorate energy harvesting efficiency, PS should employ multiple antennas, which is the case in this paper.

Wireless propagation causes a multitude of impairments like path loss, fading, shadowing, which influence drastically reliability of wireless transmission. For eNOMAu under consideration in this work, wireless channels impact an amount of scavenged energy and communication reliability. For performance assessment realistically, wireless propagation must be characterized properly to fit real-world data.  $\kappa - \mu$  shadowed fading paradigm is widely acknowledged to feature appropriately concurrent effects of fading, path loss, shadowing [8].

In summary, eNOMAu exposes advantages of high spectrum and energy efficiencies. Notwithstanding, the outage probability of eNOMAu is impacted by numerous real-world impairments such as wireless channel (path loss, shadowing, fading), ES non-linearity, and multi-antenna deployment. Thence, performance assessment of eNOMAu is essential to confirm whether eNOMAu possesses such superiority as working in such impairments. This paper proposes outage probability and throughput assessment under consideration of all these factors.



Figure 1. Energy scavenging-aided NOMA uplink communications in this paper

Wang and Men [3], eNOMAu was studied whereby multiple NOMA terminals that broadcast information to a common receiver NR need two stages (Figure 1). In stage 1, NOMA terminals utilize nonlinear energy harvesters (NLEHs) to harvest radio frequency energy from a stable PS while in stage 2, they use harvested energy to send data to NR. Wang and Men [3] showed each stage is optimized for the best performance. Nonetheless, Wang and Men [3] overlooked the explicit analysis of secrecy outage probability. The particular example of [3] with two NOMA terminals was demonstrated in [9] that presented approximated outage probability analysis. Researchers [10]-[12] studied energy scavenging-aided NOMA downlink communications (eNOMAd) in which NR sends information using NOMA to two receivers (U1 and U2). Afterwards, Le *et al.* [13] performed an extension of [10]-[12] to multiple receivers. Researchers [10]-[13] derived the approximated formulas of outage probability (OP) and throughput (TP). In addition, Le *et al.* [13] maximized sum-rate. However, researchers in [10], [11], the single-antenna NOMA device provides energy for NR. In contrast, Le *et al.* [13] the multi-antenna NOMA device supplies energy for NR. Nevertheless, researchers [10], [11], [13] utilizes unrealistic linear energy harvester (LEH). Furthermore, U1 harvests radio frequency energy from the single-antenna NR by NLEH in [12].

eNOMAd with two recipients (U1 and U2) was investigated whereby transmission to U1 is aided by a relay in [14]-[16] and by U2 in [17]-[21]. The relay and U2 in [14]-[21] scavenge power from the NOMA transmitter. Researchers [16], [17] studied NLEH at the relay in their approximated OP analysis. In the meantime, researchers [14], [19], [20] solved the aggregate capacity optimization problem. Nevertheless, Liu

*et al.* [14] considered LEH whereas Si *et al.* [19] and Garcia *et al.* [20] implemented NLEH. Researchers in [22], [23] performed an extension of [16] to multiple relays as well as selected the best relay to aid NOMA transmission from NR to U1 and U2. Furthermore, Zhai *et al.* [24] extended Agrawal *et al.* [16] to assist U2 by utilizing two relaying devices. However, Zhai *et al.* [24] overlooked the closed-form TP analysis. Instead of employing a multitude of relays in [22], [23], [25] exploited a multitude of near NOMA terminals and performed selecting solely one near NOMA terminal to help the far NOMA terminal. Another extension of Agrawal *et al.* [16] is to investigate several receivers in [26], [27]. Notwithstanding, researchers [15], [18], [21]-[27] conducted performance analysis for LEH. Moreover, researchers [28]-[30] exploited reconfigurable intelligent surface to relay messages from NR to U1 and U2 in order to maximize aggregate capacity. However, Lyu et al. [28] considered NLEH whereas [29], [30] investigated LEH. Additionally, system performance was not analyzed in [14], [19], [20], [28]-[30].

To sum up, the aforementioned publications pertinent to performance analysis in [3], [9]-[13], [15]-[26], [29], [30] investigated a trivial system model with the single-antenna PS, thence barely meliorating ES efficiency. Merely Aldababsa and Basar [27] studied several antennas employed at all users. Additionally, only trivial fading models without shadowing such as Rayleigh ([3], [12], [13], [16]-[21], [24], [25], [29]), Rician ([14], [15], [28], [30]), Weibull [26], Nakagami-m ([10], [11], [22], [23], [27]) have been considered in the previous publications. Thence, the updated publications overlooked the OP/TP analyses for the configuration in Figure 1 when considering path loss, shadowing, generalized  $\kappa - \mu$  fading, and several antennas at PS such that U1 and U2 harvest more energy, ultimately ameliorating system performance at NR. This paper pioneers in carrying out such an analysis that is useful in evaluating swiftly and maximizing system performance prior to practical deployment.

The contributions are itemized to be: (i) we recommend eNOMAu in Figure 1 in which the arbitrary number of antennas can be deployed at PS for ameliorating energy harvesting efficiency, eventually improving system performance; (ii) to evaluate communication reliability promptly, we perform the OP/TP analyses for the proposed eNOMAu considering the non-linearity of energy harvesting, the multiple antenna consideration, and different channel impairments like path loss, fading, shadowing; and (iii) we rate and maximize system performance in distinct realistic scenarios. Multiple results demonstrate a considerable performance degradation owing to non-linearity of energy scavengers and impairments of wireless propagation. Moreover, communications reliability of eNOMAu can be controlled and maximized by adopting appropriately and flexibly several specifications. Additionally, accreting a quantity of antennas improves significantly system performance. Further, the proposed eNOMAu is considerably superior to its eOMAu counterpart.

Section 2 explains the recommended eNOMAu. Subsequently, section 3 carries out the OP and TP analyses. Then, section 4 presents the asymptotic performance analysis in the regime of high transmit power. Next, section 5 analyzes the benchmark eOMAu scheme for convenience in comparing with the proposed eNOMAu. Then, section 6 discusses simulated/analytical results in different practical settings. Eventually, section 7 concludes the paper. Notable symbols are presented in Table 1.

Table 1. Notable symbols									
Symbol	Interpretation								
N(0,b)	Zero-mean and b-variance complex Gaussian random variable								
$\Gamma(\cdot)$	Complete gamma function								
$F_Q(\cdot)$	Cumulative distribution functon (CDF) of $Q$								
$\Pr{\{\cdot\}}$	Probability operator								
$\bar{F}_Q(\cdot)$	Complementary cumulative distribution function (CCDF) of $Q$								
E{·}	Expectation operator								
$f_Q(\cdot)$	Probability density function (PDF) of $Q$								
$\Theta_Q(\cdot)$	Moment generating function (MGF) of $Q$								
$\Gamma(\cdot, \cdot)$	Incomplete upper gamma function								
$C_k^l = \frac{k!}{l!(k-l)!}$	Binomial coefficient								

## Table 1. Notable symbols

## 2. ENERGY SCAVENGING-AIDED NOMA UPLINK COMMUNICATIONS

#### 2.1. System model

Figure 1 depicts eNOMAu comprising U2, U1, NR, PS. eNOMAu exemplifies uplink communications in mobile wireless systems. U2 and U1 have power limitation. Thereby, they ought to scavenge power from PS. In eNOMAu, PS provides power for operations of U2 and U1 in  $\alpha T$  time unit of Stage 1 wherein T

mentions the frame duration and  $\alpha \in (0, 1)$  means the time splitting parameter, whereas U2 and U1 conduct uplink communications using NOMA to NR in the remainder of T in stage 2. To ameliorate energy scavenging efficiency, ultimately enhancing system performance, V antennas are supposed to be deployed at PS, which is possible for high-energy PS. More particular, multi-antenna PS enables U2 and U1 to scavenge energy effectively. Nonetheless, U1, U2 and NR may be mobile terminals and thence, assumption of single antenna deployed at them is more appropriate.

#### 2.2. Channel model

Our work represents  $g_{s_v i}$  and  $g_i$  correspondingly as channel gains from the  $v^{th}$  antenna of PS to Ui and from Ui to NR where  $i = \{1, 2\}$ . It also supposes block frequency non-selective  $\kappa - \mu$  shadowed fading links. In particular, a cluster of specifications  $(\mu, \kappa, \beta, \vartheta_{xy})$  determines definitely  $g_{xy}$  with  $xy = \{s_v i, i\}$ . In other words, by changing a parameter set  $(\kappa, \mu, \beta, \vartheta_{xy})$  of such  $\kappa - \mu$  shadowed fading model, one can control flexibly different impairment levels of shadowing, path loss, fading. The parameter  $\vartheta_{xy} = \mathsf{E}\{g_{xy}\}$ represents channel power, which comprises path loss,  $\mu$  notates the quantity of multi-path groups,  $\beta$  indicates shadowing effect,  $\kappa$  indicates the Rician-K parameter. Accordingly, this model characterizes a majority of practical wireless channels. As per [8], the PDF and CDF of  $g_{xy}$  are given by

$$\mathbf{f}_{g_{xy}}\left(w\right) = \sum_{l=0}^{G} \frac{H_{l}}{\Lambda_{xy}^{\beta_{l}} \Gamma\left(\beta_{l}\right)} w^{\beta_{l}-1} e^{-\frac{w}{\Lambda_{xy}}} \quad \text{and} \quad \mathbf{F}_{g_{xy}}\left(w\right) = 1 - \sum_{l=0}^{G} \sum_{c=0}^{\beta_{l}-1} \frac{H_{l}}{\Lambda_{xy}^{c} c!} w^{c} e^{-\frac{w}{\Lambda_{xy}}}, \tag{1}$$

whereby  $\Lambda_{xy} = \frac{\vartheta_{xy}(\beta + \kappa\mu)}{\mu\beta(\kappa+1)}$ ,  $H_l = \left(\frac{\kappa\mu}{\beta + \kappa\mu}\right)^{G-l} \left(\frac{\beta}{\beta + \kappa\mu}\right)^l \mathbf{C}_G^l$ ,  $\beta_l = \beta - l$ ,  $G = \beta - \mu$  with  $\mu \leq \beta$ . To represent path loss, we model  $\vartheta_{xy}$  as  $\varrho d_{xy}^{-\sigma}$  with  $\varrho$  being fading power at 1 meter (m),  $\sigma$  being path loss decay,  $d_{xy}$  being transceiver distance [7].

Independent and identically distributed (i.i.d) fading channels between the NOMA user *i* and PS's antennas are supposed and ergo, the subscripts  $s_v i$  related to channel specifications  $(g_{s_v i}, \Lambda_{s_v i}, \vartheta_{s_v i})$  can be written shortly as si in  $(g_{si}, \Lambda_{si}, \vartheta_{si})$  if not inducing any confusion, viz.  $\epsilon_{s_v i} = \epsilon_{si}, \forall v, \epsilon = \{g, \Lambda, \vartheta\}$ .

#### 2.3. Signal representation

PS grants energy for U2 and U1 over multiple-input single-output links in Stage 1, considerably increasing amount of collected power at U2 and U1. Accordingly, the energy available at the NOMA user i is  $E_i = \rho \alpha TP \sum_{v=1}^{V} g_{s_v i}$  where P is per-antenna power of PS,  $g_{s_v i} = |h_{s_v i}|^2$  with  $h_{s_v i}$  being channel gain between the NOMA user i and the  $v^{th}$  antenna of PS, and  $\rho \in (0, 1)$  means energy converting efficiency. Power available for Stage 2 transferred from  $E_i$  is  $\frac{E_i}{(1-\alpha)T}$  due to Stage 2 prolonging  $(1-\alpha)T$  time unit. Thereby, the NOMA user i conducts transmission in Stage 2 with the following power aligned with NLEH in [6]:

$$P_{i} = \begin{cases} \frac{\rho \alpha P}{1-\alpha} \sum_{v=1}^{V} g_{s_{v}i} &, \alpha P \sum_{v=1}^{V} g_{s_{v}i} \leq \psi \\ \frac{\rho \alpha \psi}{1-\alpha} &, \alpha P \sum_{v=1}^{V} g_{s_{v}i} > \psi \end{cases} = \begin{cases} AQ_{i} &, Q_{i} \leq B \\ D &, Q_{i} > B \end{cases}$$
(2)

wherein  $\psi$  is the power saturation threshold,  $A = \frac{\rho \alpha P}{1-\alpha}$ ,  $D = \frac{\rho \alpha \psi}{1-\alpha}$ ,  $B = \frac{\psi}{\alpha P}$ , and  $Q_i = \sum_{v=1}^{V} g_{s_v i}$ .

Stage 2 is for uplink communications using NOMA where U2 and U1 conduct concurrent transmissions of  $x_1$  and  $x_2$  with powers of  $P_1$  and  $P_2$  to NR where  $\mathsf{E}\left\{|x_1|^2\right\} = \mathsf{E}\left\{|x_2|^2\right\} = 1$ . Accordingly, NR receives a signal as

$$y = h_1 \sqrt{P_1} x_1 + h_2 \sqrt{P_2} x_2 + \xi, \tag{3}$$

wherein NR suffers the noise  $\xi \sim N(0, \zeta)$ ,  $h_1$  and  $h_2$  are channel gains correspondingly pertinent to channel power gains as  $g_1 = |h_1|^2$  and  $g_2 = |h_2|^2$ .

Relied on (3), NR performs decoding  $x_1$  and  $x_2$  using NOMA principle. Two cases of the order to recover  $x_1$  and  $x_2$  are possible. If the signal from U1 is stronger than U2 ( $g_1P_1 > g_2P_2$ ), then NR firsly

recovers  $x_1$  by behaving  $x_2$  as noise. Thereby, NR restores  $x_1$  with signal-to-interference plus noise ratio (SINR) derived from (3) as

$$\tilde{\gamma}^{x_1} = \frac{g_1 P_1}{g_2 P_2 + \zeta}.\tag{4}$$

After suppressing noise which  $x_1$  generates, NR keeps recovering  $x_2$  from  $\tilde{y} = y - h_1 \sqrt{P_1} x_1 = h_2 \sqrt{P_2} x_2 + \xi$ . Accordingly, in line with  $\tilde{y}$ , NR recovers  $x_2$  with signal-to-noise ratio (SNR) to be

$$\tilde{\gamma}^{x_2} = \frac{g_2 P_2}{\zeta}.\tag{5}$$

Similarly, if the signal from U2 is stronger than U1  $(g_2P_2 > g_1P_1)$ , then NR firstly recovers  $x_2$  under consideration of  $x_1$  with the role of noise. Afterwards, NR decodes  $x_2$  with SINR derived by (3) as

$$\hat{\gamma}^{x_2} = \frac{g_2 P_2}{g_1 P_1 + \zeta}.$$
(6)

Subsequently after suppressing noise that  $x_2$  induces, NR keeps recovering  $x_1$  from  $\hat{y} = y - h_2 \sqrt{P_2} x_2 = h_1 \sqrt{P_1} x_1 + \xi$ . Thereby, in line with  $\hat{y}$ , NR decodes  $x_1$  with SNR to be

$$\hat{\gamma}^{x_1} = \frac{g_1 P_1}{\zeta}.\tag{7}$$

#### 3. PERFORMANCE ANALYSIS OF ENOMAU

This part initially makes the OP analysis of eNOMAu. The OP stands for the probability which the channel capacity lowers the predetermined transmission speed  $C_0$ . Thereafter, OP analysis is reused to attain TP analysis. Such analyses offer prompt TP/OP assessment irrespective of exhaustive simulations.

#### 3.1. OP of U1

There are three scenarios that cause U1 to be in outage:

- The 1st scenario is when the signal at NR from U1 is stronger than that from U2  $(g_1P_1 > g_2P_2)$  and NR fails to decode  $x_1$   $(\tilde{\gamma}^{x_1} < \gamma_0)$  where  $\gamma_0 = 2^{C_0/(1-\alpha)} 1$ .
- The 2nd scenario is when the signal at NR from U2 is stronger than that from U1  $(g_2P_2 > g_1P_1)$  and NR fails to decode  $x_2$   $(\hat{\gamma}^{x_2} < \gamma_0)$ .
- The 3rd scenario is when the signal at NR from U2 is stronger than that from U1  $(g_2P_2 > g_1P_1)$  and NR decodes  $x_2$  successfully  $(\hat{\gamma}^{x_2} \ge \gamma_0)$  but fails to decode  $x_1$   $(\hat{\gamma}^{x_1} < \gamma_0)$ .

The OP of U1 is thereby expressed as:

$$\Upsilon_{1} = \underbrace{\Pr\left\{g_{1}P_{1} > g_{2}P_{2}, \tilde{\gamma}^{x_{1}} < \gamma_{0}\right\}}_{\Upsilon_{11}} + \underbrace{\Pr\left\{g_{1}P_{1} < g_{2}P_{2}, \hat{\gamma}^{x_{2}} < \gamma_{0}\right\}}_{\Upsilon_{12}} + \underbrace{\Pr\left\{g_{1}P_{1} < g_{2}P_{2}, \hat{\gamma}^{x_{2}} \ge \gamma_{0}, \hat{\gamma}^{x_{1}} < \gamma_{0}\right\}}_{\Upsilon_{13}}$$
(8)

Now, we derive all terms  $(\Upsilon_{11}, \Upsilon_{12}, \Upsilon_{13})$  to complete the derivation of (8). First, inserting (4) into (8) yields.

$$\begin{split} \Upsilon_{11} &= \Pr\left\{g_{1}P_{1} > g_{2}P_{2}, \frac{g_{1}P_{1}}{g_{2}P_{2} + \zeta} < \gamma_{0}\right\} \\ &= \Pr\left\{z_{1} > z_{2}, z_{1} < \gamma_{0}z_{2} + \gamma_{0}\zeta\right\} \\ &= \Pr\left\{z_{2} < z_{1} < \gamma_{0}z_{2} + \gamma_{0}\zeta, z_{2} < \gamma_{0}z_{2} + \gamma_{0}\zeta\right\} \\ &= \begin{cases} \underbrace{\tilde{\Upsilon}_{11}}_{\Pr\left\{z_{2} < z_{1} < \gamma_{0}z_{2} + \gamma_{0}\zeta\right\}} &, \gamma_{0} \ge 1 \\ \underbrace{\Pr\left\{z_{2} < z_{1} < \gamma_{0}z_{2} + \gamma_{0}\zeta, z_{2} < \frac{\gamma_{0}\zeta}{1 - \gamma_{0}}\right\}}_{\tilde{\Upsilon}_{12}} &, \gamma_{0} < 1 \end{cases} \end{split}$$
(9)

where  $z_1 = g_1 P_1$  and  $z_2 = g_2 P_2$ .

Comment 1: One sees from (9) that since  $\gamma_0 = 2^{C_0/(1-\alpha)} - 1$ , selecting the target spectral efficiency  $C_0$  and the time portion  $\alpha$  leads to  $\gamma_0 < 1$  or  $\gamma_0 \ge 1$ , inducing  $\Upsilon_{11}$  to accept different values and eventually causing different outage levels for U1. Also, since  $\tilde{\Upsilon}_{11} > \tilde{\Upsilon}_{12}$  and  $\gamma_0$  represents the SNR/SINR threshold,  $\Upsilon_{11}$  when selecting  $C_0$  and  $\alpha$  in order for  $\gamma_0$  to be large (i.e.  $\gamma_0 \ge 1$ ) is larger than that when selecting  $C_0$  and  $\alpha$  in order for  $\gamma_0 < 1$ ).

 $\tilde{\Upsilon}_{11}$  and  $\tilde{\Upsilon}_{12}$  are represented through  $f_{z_2}(\cdot)$  and  $F_{z_1}(\cdot)$  as follows:

$$\tilde{\Upsilon}_{11} = \int_{0}^{\infty} \left[ \mathsf{F}_{z_{1}} \left( \gamma_{0} x + \gamma_{0} \zeta \right) - \mathsf{F}_{z_{1}} \left( x \right) \right] \mathsf{f}_{z_{2}} \left( x \right) dx, \quad \tilde{\Upsilon}_{12} = \int_{0}^{\frac{\gamma_{0} \zeta}{1 - \gamma_{0}}} \left[ \mathsf{F}_{z_{1}} \left( \gamma_{0} x + \gamma_{0} \zeta \right) - \mathsf{F}_{z_{1}} \left( x \right) \right] \mathsf{f}_{z_{2}} \left( x \right) dx, \quad (10)$$

where the CDF of  $z_i$ ,  $i = \{1, 2\}$ , is proved in [31] as:

$$\mathsf{F}_{z_i}\left(x\right) = \frac{B}{2} \sum_{u=1}^{U} \frac{\pi}{U} \sqrt{1 - \varphi_u^2} \mathsf{f}_{Q_i}\left(\varpi_u\right) \mathsf{F}_{g_i}\left(\frac{x}{A\varpi_u}\right) + \bar{\mathsf{F}}_{Q_i}\left(B\right) \mathsf{F}_{g_i}\left(\frac{x}{D}\right),\tag{11}$$

wherein U is a parameter of Gaussian-Chebyshev quadrature [32],  $\varpi_u = \frac{B}{2} (\varphi_u + 1)$ , and  $\varphi_u = \cos \left(\frac{2u-1}{2U}\pi\right)$ . Moreover, [31] showed  $f_{Q_i}(x)$  and  $\bar{F}_{Q_i}(x)$  as:

$$\mathbf{f}_{Q_i}(x) = \sum_{\substack{S \\ v=0}} V! \left\{ \prod_{t=0}^{G} \frac{\left(H_t\right)^{a_t}}{a_t!} \right\} \frac{x^{\phi-1}}{\Lambda_{si}^{\phi} \Gamma(\phi)} e^{-\frac{x}{\Lambda_{si}}}, \quad \bar{\mathbf{F}}_{Q_i}(x) = \sum_{\substack{S \\ v=0}} \Gamma\left(\phi, \frac{x}{\Lambda_{si}}\right) \frac{V!}{\Gamma(\phi)} \prod_{t=0}^{G} \frac{\left(H_t\right)^{a_t}}{a_t!}, \quad (12)$$

where  $\phi = \sum_{t=0}^{G} a_t \beta_t$ .

The derivative of  $\mathsf{F}_{z_i}(x)$  yields the PDF of  $z_i$  to be:

$$\mathbf{f}_{z_i}\left(x\right) = \frac{d\mathbf{F}_{z_i}\left(x\right)}{dx} = \frac{B}{2} \sum_{u=1}^{U} \sqrt{1 - \varphi_u^2} \frac{\pi \mathbf{f}_{Q_i}\left(\varpi_u\right)}{UA\varpi_u} \mathbf{f}_{g_i}\left(\frac{x}{A\varpi_u}\right) + \frac{\bar{\mathbf{F}}_{Q_i}\left(B\right)}{D} \mathbf{f}_{g_i}\left(\frac{x}{D}\right). \tag{13}$$

Inserting (11) and (13) into (10) and after some careful simplifications, one attains the explicit expression of  $\tilde{\Upsilon}_{11}$  to be:

$$\tilde{\Upsilon}_{11} = \frac{\bar{\mathsf{F}}_{Q_1}(B)\bar{\mathsf{F}}_{Q_2}(B)}{D}\Psi(D,D) + \frac{\pi B}{2U}\sum_{u=1}^{U}\sqrt{1-\varphi_u^2} \left\{ \frac{\mathsf{f}_{Q_1}(\varpi_u)\bar{\mathsf{F}}_{Q_2}(B)}{D}\Psi(A\varpi_u,D) + \frac{\mathsf{f}_{Q_2}(\varpi_u)\bar{\mathsf{F}}_{Q_1}(B)}{A\varpi_u}\Psi(D,A\varpi_u) + \frac{\pi B}{2U}\sum_{v=1}^{U}\sqrt{1-\varphi_v^2}\frac{\mathsf{f}_{Q_1}(\varpi_u)\mathsf{f}_{Q_2}(\varpi_v)}{\varpi_v A}\Psi(A\varpi_u,A\varpi_v) \right\},$$
(14)

where  $\varphi_v$  and  $\overline{\omega}_v$  are defined in the same manner as  $\varphi_u$  and  $\overline{\omega}_u$  whilst the function  $\Psi(\cdot, \cdot)$  has a closed form as (17).

 $\Psi\left(\cdot,\cdot\right)$  is a function of two arguments (I,J) as:

$$\Psi(I,J) = \int_{0}^{\infty} \left[ \mathsf{F}_{g_1}\left(\frac{\gamma_0 x + \gamma_0 \zeta}{I}\right) - \mathsf{F}_{g_1}\left(\frac{x}{I}\right) \right] \mathsf{f}_{g_2}\left(\frac{x}{J}\right) dx.$$
(15)

Invoking  $f_{g_i}(\cdot)$  and  $F_{g_i}(\cdot)$  in (1) and using the binomial expansion, one simplifies  $\Psi(I, J)$  as:

$$\Psi(I,J) = \int_{0}^{\infty} \left[ \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \frac{H_{k}}{(\Lambda_{1}I)^{u}u!} \left( x^{u}e^{-\frac{x}{\Lambda_{1}I}} - e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}I}} \gamma_{0}^{u}(x+\zeta)^{u}e^{-\frac{\gamma_{0}x}{\Lambda_{1}I}} \right) \right] \times \\ \left[ \sum_{m=0}^{G} \frac{H_{m}J^{1-\beta_{m}}}{\Lambda_{2}^{\beta_{m}}\Gamma(\beta_{m})} x^{\beta_{m}-1}e^{-\frac{x}{\Lambda_{2}J}} \right] dx \\ = \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \sum_{m=0}^{G} \frac{H_{k}H_{m}J^{1-\beta_{m}}}{(\Lambda_{1}I)^{u}u!\Lambda_{2}^{\beta_{m}}\Gamma(\beta_{m})} \int_{0}^{\infty} \left[ x^{u+\beta_{m}-1}e^{-\left(\frac{1}{\Lambda_{1}I} + \frac{1}{\Lambda_{2}J}\right)x} - e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}I}} \gamma_{0}^{u}e^{-\left(\frac{\gamma_{0}}{\Lambda_{1}I} + \frac{1}{\Lambda_{2}J}\right)x} x^{\beta_{m}-1} \sum_{l=0}^{u} \mathbf{C}_{u}^{l}x^{l}\zeta^{u-l} \right] dx \\ = \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \sum_{m=0}^{G} \frac{H_{k}H_{m}J^{1-\beta_{m}}}{(\Lambda_{1}I)^{u}u!\Lambda_{2}^{\beta_{m}}\Gamma(\beta_{m})} \left[ \int_{0}^{\infty} x^{u+\beta_{m}-1}e^{-\left(\frac{1}{\Lambda_{1}I} + \frac{1}{\Lambda_{2}J}\right)x} dx - e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}I}} \gamma_{0}^{u} \sum_{l=0}^{u} \mathbf{C}_{u}^{l}\zeta^{u-l} \int_{0}^{\infty} x^{l+\beta_{m}-1}e^{-\left(\frac{\gamma_{0}}{\Lambda_{1}I} + \frac{1}{\Lambda_{2}J}\right)x} dx \right].$$

The last integrals in (16) are solved with the help of [33] (3.351.3) Grad, eventually leading to the closed form of  $\Psi(I, J)$  as:

$$\Psi(I,J) = \sum_{m=0}^{G} \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \frac{H_{k}H_{m}J^{1-\beta_{m}}}{(\Lambda_{1}I)^{u}u!\Lambda_{2}^{\beta_{m}}\Gamma(\beta_{m})} \left[ \Gamma\left(u+\beta_{m}\right) \left(\frac{1}{\Lambda_{1}I}+\frac{1}{\Lambda_{2}J}\right)^{-(u+\beta_{m})} - e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}I}}\gamma_{0}^{u} \sum_{l=0}^{u} C_{u}^{l}\zeta^{u-l}\Gamma\left(l+\beta_{m}\right) \left(\frac{\gamma_{0}}{\Lambda_{1}I}+\frac{1}{\Lambda_{2}J}\right)^{-(l+\beta_{m})} \right].$$
(17)

Subsequently, by exploiting the Gaussian-Chebyshev quadrature, one tightly approximates  $\tilde{\Upsilon}_{12}$  as:

$$\tilde{\Upsilon}_{12} = \frac{\gamma_0 \zeta}{2 (1 - \gamma_0)} \sum_{u=1}^U \frac{\pi}{U} \sqrt{1 - \varphi_u^2} \left[ \mathsf{F}_{z_1} \left( \gamma_0 \chi_u + \gamma_0 \zeta \right) - \mathsf{F}_{z_1} \left( \chi_u \right) \right] \mathsf{f}_{z_2} \left( \chi_u \right), \tag{18}$$

where  $\chi_u = \frac{\gamma_0 \zeta}{2(1-\gamma_0)} (\varphi_u + 1)$ . Next, inserting  $\hat{\gamma}^{x_2}$  in (6) into  $\Upsilon_{12}$  yields.

$$\Upsilon_{12} = \Pr\left\{g_1 P_1 < g_2 P_2, \frac{g_2 P_2}{g_1 P_1 + \zeta} < \gamma_0\right\}.$$
(19)

By comparing  $\Upsilon_{12}$  in (19) with  $\Upsilon_{11}$  in (9), one recognizes that the explicit formula of  $\Upsilon_{12}$  is obtained from that of  $\Upsilon_{11}$  by interchanging  $(\Lambda_1, \Lambda_{s1})$  and  $(\Lambda_2, \Lambda_{s2})$ . Accordingly, the derivation of  $\Upsilon_{12}$  is omitted for compactness.

Finally, inserting  $\hat{\gamma}^{x_2}$  in (6) and  $\hat{\gamma}^{x_1}$  in (7) into  $\Upsilon_{13}$  yields.

$$\begin{split} \Upsilon_{13} &= \Pr\left\{g_{1}P_{1} < g_{2}P_{2}, \frac{g_{2}P_{2}}{g_{1}P_{1} + \zeta} \ge \gamma_{0}, \frac{g_{1}P_{1}}{\zeta} < \gamma_{0}\right\} \\ &= \Pr\left\{g_{1}P_{1} < g_{2}P_{2}, g_{2}P_{2} \ge \gamma_{0}g_{1}P_{1} + \gamma_{0}\zeta, g_{1}P_{1} < \gamma_{0}\zeta\right\} \\ &= \Pr\left\{g_{2}P_{2} \ge \gamma_{0}g_{1}P_{1} + \gamma_{0}\zeta, g_{1}P_{1} < \gamma_{0}\zeta\right\} \\ &= \int_{0}^{\gamma_{0}\zeta} [1 - \mathsf{F}_{z_{2}}\left(\gamma_{0}x + \gamma_{0}\zeta\right)]\mathsf{f}_{z_{1}}\left(x\right)dx \\ &= \mathsf{F}_{z_{1}}\left(\gamma_{0}\zeta\right) - \int_{0}^{\gamma_{0}\zeta} \mathsf{F}_{z_{2}}\left(\gamma_{0}x + \gamma_{0}\zeta\right)\mathsf{f}_{z_{1}}\left(x\right)dx. \end{split}$$
(20)

 $\int_{0}^{\gamma_{0}\zeta} \mathsf{F}_{z_{2}}(\gamma_{0}x + \gamma_{0}\zeta) \mathfrak{f}_{z_{1}}(x) dx \text{ has a tight approximation by employing Gaussian-Chebyshev quadrature, yielding.}$ 

$$\Upsilon_{13} = \mathsf{F}_{z_1}\left(\gamma_0\zeta\right) - \frac{\gamma_0\zeta}{2} \sum_{u=1}^U \frac{\pi}{U} \sqrt{1 - \varphi_u^2} \mathsf{F}_{z_2}\left(\gamma_0\delta_u + \gamma_0\zeta\right) \mathsf{f}_{z_1}\left(\delta_u\right),\tag{21}$$

where  $\delta_u = \frac{\gamma_0 \zeta}{2} (\varphi_u + 1).$ 

## 3.2. OP of U2

- There are three scenarios that cause U2 to be in outage:
- The 1st scenario is when the signal at NR from U2 is stronger than that from U1  $(g_2P_2 > g_1P_1)$  and NR fails to decode  $x_2$   $(\hat{\gamma}^{x_2} < \gamma_0)$ .
- The 2nd scenario is when the signal at NR from U1 is stronger than that from U2  $(g_1P_1 > g_2P_2)$  and NR fails to decode  $x_1$   $(\tilde{\gamma}^{x_1} < \gamma_0)$ .
- The 3rd scenario is when the signal at NR from U1 is stronger than that from U2  $(g_1P_1 > g_2P_2)$  and NR decodes  $x_1$  successfully  $(\tilde{\gamma}^{x_1} \ge \gamma_0)$  yet fails to recover  $x_2$   $(\tilde{\gamma}^{x_2} < \gamma_0)$ .

The OP of U2 is thereby expressed as:

$$\Upsilon_{2} = \underbrace{\Pr\left\{g_{1}P_{1} < g_{2}P_{2}, \hat{\gamma}^{x_{2}} < \gamma_{0}\right\}}_{\Upsilon_{21}} + \underbrace{\Pr\left\{g_{1}P_{1} > g_{2}P_{2}, \tilde{\gamma}^{x_{1}} < \gamma_{0}\right\}}_{\Upsilon_{22}} + \underbrace{\Pr\left\{g_{1}P_{1} > g_{2}P_{2}, \tilde{\gamma}^{x_{1}} \ge \gamma_{0}, \tilde{\gamma}^{x_{2}} < \gamma_{0}\right\}}_{\Upsilon_{23}}.$$
 (22)

By comparing (22) with (8), one infers that  $\Upsilon_{21} = \Upsilon_{12}$  and  $\Upsilon_{22} = \Upsilon_{11}$ . Moreover, inserting  $\tilde{\gamma}^{x_1}$  in (4) and  $\tilde{\gamma}^{x_2}$  in (5) into (22) yields.

$$\Upsilon_{23} = \Pr\left\{g_1 P_1 > g_2 P_2, \frac{g_1 P_1}{g_2 P_2 + \zeta} \ge \gamma_0, \frac{g_2 P_2}{\zeta} < \gamma_0\right\}.$$
(23)

By comparing  $\Upsilon_{23}$  with  $\Upsilon_{13}$  in (20), one recognizes that the explicit formula of  $\Upsilon_{23}$  is obtained from that of  $\Upsilon_{13}$  by interchanging  $(\Lambda_1, \Lambda_{s1})$  and  $(\Lambda_2, \Lambda_{s2})$ . Accordingly, the derivations of  $\Upsilon_{21}$ ,  $\Upsilon_{22}$ , and  $\Upsilon_{23}$  are omitted for compactness. Moreover, similar to  $\Upsilon_1$ , one sees that the outage level of U2,  $\Upsilon_2$ , can be adjusted by selecting properly  $C_0$  and  $\alpha$ .

*Comment 2*: Both  $\Upsilon_1$  and  $\Upsilon_2$  are functions of specifications  $(C_0, \alpha, P, V, \psi, \rho)$ . This implies U1 and U2 is able to attain target performances by properly choosing these specifications.

#### 3.3. Throughput

In delay-constrained communication, the throughput of Ui for eNOMAu is computed as:

$$\Delta_i = (1 - \alpha)C_0 \left(1 - \Upsilon_i\right). \tag{24}$$

One sees from (24) that the TP of U*i* is jointly specified by parameters  $(C_0, \alpha, P, V, \psi, \rho)$  since this cluster impacts  $\Upsilon_i$ . Accordingly, the expected TP is obtained by appropriately choosing such parameters based on their preset value ranges.

#### 4. ASYMPTOTIC ANALYSIS OF ENOMAU

This section studies the performance upper-bound of eNOMAu corresponding to high transmission power  $(P \to \infty)$ . In such a regime, energy harvester definitely saturates and ergo,  $P_i \to D$  with  $i = \{1, 2\}$ . Accordingly, the CDF and PDF of  $z_i = g_i D$  reduce to  $\mathsf{F}_{z_i}(x) = \mathsf{F}_{g_i}\left(\frac{x}{D}\right)$  and  $\mathsf{f}_{z_i}(x) = \frac{1}{D}\mathsf{f}_{g_i}\left(\frac{x}{D}\right)$ , correspondingly, when  $P \to \infty$ . Therefore, the OP of Ui is summarized to be:

$$\Upsilon_i^{\infty} = \Upsilon_{i1}^{\infty} + \Upsilon_{i2}^{\infty} + \Upsilon_{i3}^{\infty}, \tag{25}$$

where  $\Upsilon_{11}^{\infty} = \Upsilon_{22}^{\infty}$ ,  $\Upsilon_{12}^{\infty} = \Upsilon_{21}^{\infty}$ , the explicit expressions of  $\Upsilon_{12}^{\infty}$  and  $\Upsilon_{23}^{\infty}$  are obtained from those of  $\Upsilon_{11}^{\infty}$  and  $\Upsilon_{13}^{\infty}$  by interchanging  $(\Lambda_1, \Lambda_{s1})$  and  $(\Lambda_2, \Lambda_{s2})$ , and

$$\Upsilon_{11}^{\infty} = \begin{cases} \tilde{\Upsilon}_{11}^{\infty} &, \gamma_0 \ge 1\\ \tilde{\Upsilon}_{12}^{\infty} &, \gamma_0 < 1 \end{cases}$$
(26)

with

$$\tilde{\Upsilon}_{11}^{\infty} = \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \sum_{m=0}^{G} \frac{H_{k}H_{m}D^{-u-\beta_{m}}}{\Lambda_{1}^{u}u!\Lambda_{2}^{\beta_{m}}\Gamma\left(\beta_{m}\right)} \left[\Gamma\left(u+\beta_{m}\right)\left\{\left(\frac{1}{\Lambda_{1}}+\frac{1}{\Lambda_{2}}\right)\frac{1}{D}\right\}^{-u-\beta_{m}}-e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}D}}\gamma_{0}^{u}\sum_{l=0}^{u} \mathsf{C}_{u}^{l}\zeta^{u-l}\Gamma\left(l+\beta_{m}\right)\left\{\left(\frac{\gamma_{0}}{\Lambda_{1}}+\frac{1}{\Lambda_{2}}\right)\frac{1}{D}\right\}^{-l-\beta_{m}}\right]$$
(27)

$$\tilde{\Upsilon}_{12}^{\infty} = \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \sum_{m=0}^{G} \frac{H_{k}H_{m}D^{-u-\beta_{m}}}{\Lambda_{1}^{u}u!\Lambda_{2}^{\beta_{m}}\Gamma\left(\beta_{m}\right)} \left[ \Phi\left(\frac{\gamma_{0}\zeta}{1-\gamma_{0}}, u+\beta_{m}-1, \left[\frac{1}{\Lambda_{1}}+\frac{1}{\Lambda_{2}}\right]\frac{1}{D}\right) - e^{-\frac{\gamma_{0}\zeta}{\Lambda_{1}D}}\gamma_{0}^{u} \sum_{l=0}^{u} \mathsf{C}_{u}^{l}\zeta^{u-l}\Phi\left(\frac{\gamma_{0}\zeta}{1-\gamma_{0}}, l+\beta_{m}-1, \left[\frac{\gamma_{0}}{\Lambda_{1}}+\frac{1}{\Lambda_{2}}\right]\frac{1}{D}\right) \right]$$

$$(28)$$

$$\tilde{\Delta}_{13}^{\infty} = \sum_{k=0}^{G} \sum_{u=0}^{\beta_{k}-1} \sum_{m=0}^{G} \sum_{l=0}^{u} \frac{\mathsf{C}_{u}^{l} \Lambda_{1}^{-\beta_{m}} \zeta^{u-l} H_{m} H_{k}}{\Gamma\left(\beta_{m}\right) u! D^{u+\beta_{m}+1}} \left(\frac{\gamma_{0}}{\Lambda_{2}}\right)^{u} e^{-\frac{\gamma_{0}\zeta}{\Lambda_{2}D}} \Phi\left(\gamma_{0}\zeta, l+\beta_{m}-1, \left[\frac{\gamma_{0}}{\Lambda_{2}}+\frac{1}{\Lambda_{1}}\right] \frac{1}{D}\right)$$
(29)

$$\Phi(a,b,c) = \frac{b!}{c^{b+1}} - e^{-ac} \sum_{v=0}^{b} \frac{b!}{v!} \frac{a^v}{c^{b-v+1}}.$$
(30)

## 5. ENERGY SCAVENGING-AIDED ORTHOGONAL MULTIPLE ACCESS UPLINK COMMUNI-CATIONS (EOMAU)

In energy scavenging-aided orthogonal multiple access uplink communications (eOMAu), Stage 2 is separated equally into two sub-stages during which U1 and U2 transmit their information sequentially and directly to NR. Therefore, NR receives the signal from Ui as  $y_i = h_i \sqrt{P_i} + \xi_i$  where  $\xi_i$  is the noise at NR and  $i = \{1, 2\}$ . Accordingly, the channel capacity that Ui achieves is  $R_i = \frac{1-\alpha}{2} \log_2 \left(1 + \frac{g_i P_i}{\zeta}\right)$  where the factor  $\frac{1-\alpha}{2}$  before the logarithm is since Ui transmits only in  $\frac{1-\alpha}{2}T$ . Consequently, the OP of Ui is:

$$\Upsilon_{i}^{OMA} = \Pr\left\{\mathsf{R}_{i} < C_{0}\right\} = \Pr\left\{\frac{g_{i}P_{i}}{\zeta} < \tilde{\gamma}_{0}\right\} = \mathsf{F}_{z_{i}}\left(\tilde{\gamma}_{0}\zeta\right),\tag{31}$$

where  $\tilde{\gamma}_0 = 2^{2C_0/(1-\alpha)} - 1$ .

One notes that eOMAu is deemed as a baseline transmission scheme as compared to eNOMAu. Given the closed-form formula of  $\Upsilon_i^{OMA}$ , it is convenient in quickly comparing the performances between eOMAu and eNOMAu from which the advantages of NOMA are exposed promptly.

#### 6. EVALUATIONS

This section discusses multiple analytical/simulated findings to rate outage probabilities of U1 and U2 in eNOMAu and its eOMAu counterpart. The analytical formulas derived in sections 3-5 yield analytical findings (Ana.). Also, Monte-Carlo simulation is run, yielding simulated findings (Sim.). Comparing 'Sim.' with 'Ana.' validates theoretical derivations. Since OP and TP are linearly proportional to each other, TP is an one-by-one mapping of OP. Accordingly, this section presents merely outage probabilities of U1 and U2.

Terminals's positions are illustrated as NR (50,0) m, U1 (0,0) m, U2 (-10,15) m, PS (-15,0) m. Unless otherwise addressed, parameters are adopted as  $(\kappa, \beta, \mu) = (3, 4, 2)$ ,  $\rho = 10^{-2}$ ,  $\psi = -10$  dB,  $\alpha = 0.4$ ,  $\sigma = 3$ , P = 15 dB,  $C_0 = 0.5$  bps/Hz,  $\rho = 0.7$ , V = 4, and  $\zeta = -90$  dBm. Findings in subsequent figures demonstrate that *i*) analysis matches simulation, confirming preciseness of expressions obtained in sections 3-5; *ii*) U1 outperforms U2, which makes sense since U1 is nearer to PS and NR than U2.

Figure 2(a) demonstrates OPs of U1 and U2 versus P, which unveils performance enhancement with accreting P for both U1 and U2. This makes sense owing to increasing scavenged energy. Further, eNOMAu significantly outperforms its eOMAu counterpart over the whole range of P, which exposes the advantage of NOMA in comparison with OMA. Also, Figure 2(b) reveals outage performances of U1 and U2 versus  $\psi$ . One recognizes that the performances of both U1 and U2 are ameliorated with accreting  $\psi$ , as anticipated, for both

eNOMAu and eOMAu. Moreover, U1 and U2 saturate at high  $\psi$  because NLEH coincides LEH. Further, U1 and U2 are in a complete outage for low  $\psi$ , as anticipated. Furthermore, similar to Figure 2(a), findings in Figure 2(b) illustrate that eNOMAu considerably outperforms eOMAu for any  $\psi$ .

Figure 3 exposes OPs of U1 and U2 against V (Figure 3(a)) and  $\rho$  (Figure 3(b)). One expects that accreting V and  $\rho$  facilitates U1 and U2 in harvesting more energy and as a result, mitigating OPs of both U1 and U2. Figure 3 unveils exactly such an expectation wherein accreting V and  $\rho$  dramatically improves performances of both U1 and U2. Further, similar to Figure 2, the results in Figure 3 illustrate that eNOMAu is superior to its eOMAu counterpart over the whole range of V and  $\rho$ , which again illustrates the advantage of NOMA as compared to OMA.

Figure 4 reveals outage performances of U1 and U2 versus  $\alpha$  (Figure 4(a)) and  $C_0$  (Figure 4(b)). One observes from Figure 4(a) that one can optimize  $\alpha$  to reach minimum OPs for U1 and U2, and for eNOMAu and eOMAu. The optimal  $\alpha$  is for poising durations for ES and transmission. Additionally, Figure 4(b) illustrates outage increase with increasing  $C_0$  for both U1 and U2 as well as both eNOMAu and eOMAu, as expected. As analyzed in section 3, the SNR/SINR threshold  $\gamma_0$  is controlled jointly by  $C_0$  and  $\alpha$ . Moreover, the analysis in section 3 exposes that  $\gamma_0 \geq 1$  and  $\gamma_0 < 1$  cause different outage levels for eNOMAu. As such, the results in Figure 4(a) and Figure 4(b) make sense in that eNOMAu is not always better than eOMAu. More specifically, Figure 4(a) unveils that the performance of U1 (or U2) in eNOMAu outperforms that in eOMAu when  $\alpha < 0.47$  (or  $\alpha < 0.53$ ) whilst Figure 4(b) illustrates that the performance of U2 in eNOMAu outperforms that in eOMAu for any  $C_0$  but the performance of U1 in eNOMAu outperforms that in eOMAu only for  $C_0 < 0.57$  bps/Hz or  $C_0 > 1.29$  bps/Hz.



Figure 2. Influence of (a) OP versus P and (b) OP versus  $\psi$ 



Energy scavenging-aided NOMA uplink communications: performance analysis (Huu Q. Tran)

 $\kappa - \mu$  shadowed fading specified by parameters  $(\kappa, \beta, \mu)$ , which impact OPs of U1 and U2, are demonstrated in Figure 5 in which Figure 5(a) shows the impact of  $\beta$  while Figure 5(b) demonstrates the effect of  $\kappa$ . This figure reveals that the outage performances of U1 and U2 are ameliorated with accreting  $(\beta, \kappa, \mu)$ , as expected, for both eNOMAu and eOMAu. Interestingly, the performance improvement of eNOMAu with increasing  $\mu$  is considerably higher than that of eOMAu, showing the dominance of NOMA to OMA when channels are less severe (i.e.,  $\mu$  increases).



Figure 4. Influence of (a) OP versus  $\alpha$  and (b) OP versus  $C_0$ 



Figure 5. Influence of (a) OP versus  $\beta$  and (b) OP versus  $\kappa$ 

## 7. CONCLUSION

The paper analyzed the TP/OP of the suggested eNOMAu considering realistic operation conditions (multiple antennas, shadowing, NLEH, fading, path loss). The proposed analysis provides the explicit expressions that revealed directly complete comprehension of the proposed eNOMAu and rated system performance quickly in multiple sets of pivotal specifications. A multitude of findings revealed that ES nonlinearity drastically deteriorates system performance. Moreover, am expected performance can be reached by appropriately adopting specifications ( $C_0$ ,  $\alpha$ , P, V,  $\psi$ ,  $\rho$ ). Remarkably, eNOMAu attains optimum performance by properly selecting  $\alpha$ . Furthermore, the performance of eNOMAu is dramatically enhanced with accreting V and better channel conditions. Moreover, eNOMAu is significantly superior to its eOMAu counterpart.

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This journal uses the Contributor Roles Taxonomy (CRediT) to recognize individual author contributions, reduce authorship disputes, and facilitate collaboration.

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C : Conceptualization	I : Investigation									Vi	: Vis	sualizat	ion	
So : Software	D : Data Curation								P : Project Administrati					

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### **CONFLICTS OF INTEREST**

The authors declare no conflict of interest in this manuscript.

#### **INFORMED CONSENT**

We have obtained informed consent from all individuals included in this study.

#### ETHICAL APPROVAL

Not applicable.

#### DATA AVAILABILITY

Data availability is not applicable to this paper as no new data were created or analyzed in this study.

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930

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