

## Particle Filtering Approach for GNSS RAIM and FPGA Implementation

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### Abstract

The integrity monitoring system, as an integral part of aviation navigation system for global navigation satellite system (GNSS), should detect and isolated Failures or faults caused by system failures to maintain the integrity of the GNSS. The pseudorange residual noise of navigation satellites does not completely follow the Gaussian distribution, the performance of traditional filtering algorithms (such as the Kalman filtering) may be reduced due to non-Gaussian noise. The particle filter algorithm has great advantage to dealing with the nonlinear and non-Gaussian system. in this paper, the particle filter algorithm is applied to GNSS receiver autonomous integrity monitoring(RAIM) to detect the fault of navigation satellite. Firstly, Log likelihood ratio (LLR) testing is established; and then, the consistency between the state estimation of the main particle filter and the auxiliary particle filter is checked to determine whether the navigation satellite has failed; finally, the novel RAIM algorithm is undertaken by field programmable gate array (FPGA), the modules of the proposed RAIM algorithm is implemented. The effectiveness of the proposed approach is illustrated in a problem of GPS (Global Positioning System) autonomous integrity monitoring system, the algorithm and its implementation can be embeded in GNSS receiver.

**Keywords:** Global Navigation Satellite System (GNSS), Receiver Autonomous Integrity Monitoring (RAIM), particle filter, Global Positioning System (GPS), Field Programmable Gate Array (FPGA)

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### 1. Introduction

Fault detection (FD) is usually detected by real-time sensor measurements. In various fields, real-time detection of faults plays an important role in an estimated system. For a stochastic system, the fault detection method is mostly based on a linear system, assuming that noise and interference obey a Gaussian distribution. In this regard, the Kalman filter (KF) is often chosen as the state estimator [1-4]. State estimation of nonlinear systems under non-Gaussian noise is a difficult problem to solve. Usually, It is difficult to analyze and express the optimal solution. Sub-optimal solutions can be approximated to some form, such as Extended Kalman Filtering (EKF). Currently, Particle filtering is widely concerned due to its ability to handle nonlinear system or measurement noise with any probability distribution [5].

Fault detection and exclusion play a vital role in practical applications, especially in Global Navigation Satellite Systems (GNSS) such as aircraft and missile navigation. Failure to detect and exclude failures that may cause risks to the accuracy and integrity of GNSS will result in a continuous risk of navigation systems and significant losses. Fault detection and exclusion mainly considers the probability of satellites sending incorrect navigation signals to users. Integrity means that the system can promptly provide users with warnings about when they should not be used. The response time of the GPS control segment usually exceeds 15 minutes, so it is necessary to apply effective RAIM in advance to cope with sporadic satellite pseudorange error[6-10]. Actually, GNSS measurement errors do not fully follow the Gaussian distribution. Conventional snapshot RAIM are difficult to detect faults, and various filtering algorithms such as the KF presume that the measurement error and noise follow a Gaussian distribution. If the assumptions are incorrect, the performance of algorithm will also be degraded. The particle filter algorithm is suitable for nonlinear system or observation noise with

any probability distribution and can be used to detect the integrity of GNSS [11-15].

In this paper, the principle of particle filter is introduced at first. The LLR method based on particle filter and the common methods of fault detection and isolation are introduced. Then, the GPS system's system and measurement equations are described. The next section, the GPS RAIM system and its availability are given by numerical simulation. Finally, the RAIM algorithm based on FPGA is given, and describe the conclusion.

## 2. Particle Filter Algorithm

In this section, a brief explanation of a PF will be given. PF, also known as the sequential Monte Carlo method, is a statistical filtering method based on the Monte Carlo method and recursive Bayesian estimation. It approximates the required probability density function (PDF) by swarms of points in the state space. These points are called particles. PF is a nonlinear filter method for nonlinear and non-Gaussian system, which is that choosing swarms of limited weighted points to form the discrete random measure to describe the posterior probability distribution of the state PF is easily implemented in different nonlinear system because it is independent of the system model [16-19].

The dynamic state space model is used in the PF algorithm, and the state model is employed to describe the dynamic system model. PF algorithm was first proposed by Gordon and Salmond in 1993, and was known as SIR (Sampling importance resampling). Its dynamic state space model is as follows:

The state function:

$$X_k = f(X_{k-1}, \mu_{k-1}) \quad (1)$$

The measurement function:

$$Y_k = g(X_k, V_k) \quad (2)$$

Where  $X_k$  is a state vector at instant  $k$ ,  $Y_k$  is measurement vector at instant  $k$ ,  $\mu_k$  and  $V_k$  are process noise vector and measurement noise, respectively, both are random errors and independent of each other.  $f(\cdot, \cdot)$  is state transition function.  $g(\cdot, \cdot)$  is measurement function.

The steps of standard PF algorithm can be summarized as follows:

(1) Initialization. calculating the prior probability  $p(x_0)$ , and generates the initial set of  $N$  samples/particles, and that is  $\{x_0^i\}_{i=1}^{N_s}$ . And the weight of each particle is  $1/N_s$ .

(2) State prediction: the weight of sampling  $N$  particles is  $\{w_{k-1}(i) : i=1, 2, \dots, N\}$  from the PDF of system noise  $w_{k-1}$ . Using these samples to generate new swarm of  $\{x_{k|k-1}(i) : i=1, 2, \dots, N\}$ , which is approximated the predicted PDF  $p(x_k | Y_{k-1})$ .

Where,

$$x_{k|k-1}(i) = f_{k-1}(x_{k-1}(i), w_{k-1}(i)) \quad (3)$$

(3) State update. Assigning each particle of  $x_{k|k-1}(i)$  the weight of  $w_k(i)$  for  $i=1, 2, \dots, N$ , after the measurement of  $y_k$  is attained. The weights are calculated as follow:

$$w_k(i) = \frac{p(y_k | x_{k|k-1}(i))}{\sum_{j=1}^N p(y_k | x_{k|k-1}(j))} \quad (4)$$

Then, the normalized weight of the  $i$  th particle is calculated as follow:

$$w_k^i = w_k^i / \sum_{i=1}^{N_s} w_k^i \quad (5)$$

The least square estimate of the unknown parameter  $x$  can be shown to be:

$$\hat{x}_k = \sum_{i=1}^{N_s} w_k^i x_k^i \quad (6)$$

(4) Resampling. after a few iterations, most of the particle's weight will become very small until it becomes 0, and only a small amount of particle weight will become particularly large, resulting in particle degradation. We rely on the method of resampling. After resampling, the new set of particles is:

$$\{x_{0,k}^s, i = 0, 1, \dots, N_s\}$$

(5) Estimation. Using the state function  $f(\cdot, \cdot)$  to estimate the next state parameter  $x_{k+1}^i$ .

(6) Return to step 2, then  $k = k + 1$ . And the steps of prediction, updation and resampling are executed and the iteration recursively applied at each time  $k$ .

### 3. RAIM Based on Particle Filter Algorithm

In life-related navigation application services, integrity issues are very important. Once an error occurs, the consequences can be very serious. Therefore, Faults must be detected as quickly as possible. In this paper, we design the FDI system for GPS signal integrity monitoring. RAIM can use the redundant information of satellites to detect and isolate the fault satellites.

GPS state and Observation Equation can be shown as follows [20].

$$X_k = F_{k-1} X_{k-1} + \mu_{k-1} \quad (7)$$

$$\rho^i(k) = R^i(k) + c * \Delta \delta^i + T^i(k) + I^i(k) + E^i(k) + v^i(k) \quad (8)$$

The RAIM based on PF algorithm is modularly designed by field programmable gate array (FPGA). FPGA can perform larger scale calculation at the same time, and can execute the algorithm in parallel, which has a great advantage for computing swarms of particles in PF algorithm for shorter time. It has the limitation for FPGA to process floating point numbers, so the soft core processor of Microblaze is employed to FPGA. The RAIM algorithm is decomposed into two parts, the logical part and the soft-core part. The soft-core for the algorithm also consists of two parts, the part of weight calculation and the part of log-likelihood ratio (LLR) calculation. The reason is that the module of weight calculation has exponential operation, and the module of LLR contains logarithm operation. It could be easier to implement by using the soft core on FPGA. The logical part for the algorithm includes five parts: the random noise generation module, the particle state calculation module, the resample module, the fault detection and the fault isolation modules, which include lots of matrix and summation computation. It could improve the computing speed of the program on FPGA. After meeting the precision, the floating point numbers should be transformed into fixed-point numbers for FPGA to give full play in computation.

The structure of the algorithm on FPGA is as follows.



The stream of data produced by the shift register is determined by the current state. And the output sequence is periodical because of the finite number of possible states in the register. The maximum cycle of the output sequence is  $2^{n-1}$ . However, an LFSR with a well-selected feedback function can generate a randomly displayed bit sequence with a long period. In this paper, the n is set the number 10, and we can design m pseudo-random number generators, and output the result of the summation of generators. The m in this module is 8, and the initial value, which is called the seed, is different from each another. Figure 2 shows the simulation of the random noise generator.

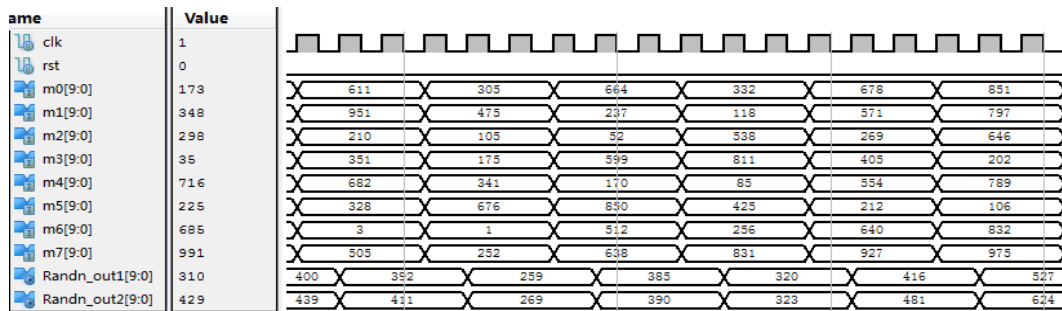


Figure 2. The simulation of random noise generator

As illustrated in Figure 2, the Randn\_out1 and Randn\_out2 give the two output ports respectively. The rst is the reset signal and the clk is the clock signal. The m0, m1, ..., m7 present the 8 pseudo-random number generators, each of which generates the pseudo-random numbers. Importing the two channels generated random numbers to Matlab program and then calculate the distribution of each channel random numbers.

**4.2. Fault Detection Module**

In this module, it should judge whether the fault detection function  $\beta_k$  exceeds detection the threshold  $\tau$ . If  $\beta_k > \tau$ , it means that a fault has occurred and the module could get the fault occurrence time t. If  $\beta_k < \tau$ , it means there is no fault in GPS navigation system. The simulation result of this module is shown in Figure 3.

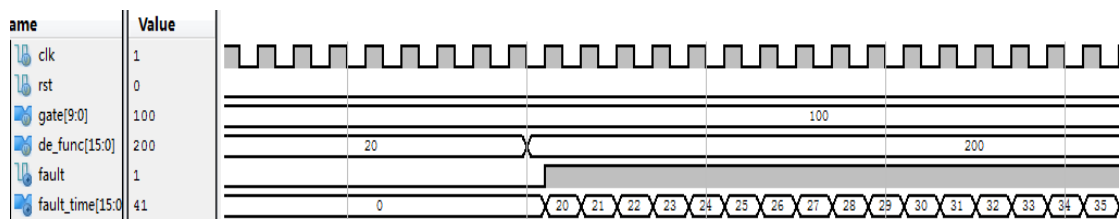


Figure 3. The simulation result of fault detection module

In simulation, the threshold is set  $\tau=100$ , that is, the internal signal gate is valued 100. The rst is the reset signal, and the clk is the clock signal. The de\_func is an input port of the value of fault detection function  $\beta_k$  to compare with the threshold. The port of fault is the enable signal port, which means that if the fault is detected, then the output of fault signal is equal 1. The fault\_time port outputs the time of fault occurrence. From Figure 3, it is shown that there is no fault occurred until the time is 20, when the de\_func is 200 at the time of 20 and exceeds the  $\tau$ . Then, the output of fault signal is set to 1 in order to indicate that the system has detected the fault.

### 4.3. Fault Isolation Module

The fault satellite could be found in this module. The fault isolation function can be expressed as:

$$satnum = \arg \max_{1 \leq q \leq Q} S(q)_{t_a}^k \tag{9}$$

Where,  $Q=m+1$ , and  $m$  is the number of visible satellites,  $S_{t_a}^k$  is the cumulative LLR of the main particle filter and the auxiliaries particle filter, where  $t_a$  is a time where the satellites' fault is detected. And  $satnum$  is the number of the fault satellite. According to the function, the fault isolation is achieved by getting the maximum value of all cumulative LLRs.

The simulation of the fault isolation module is shown in Figure 4.

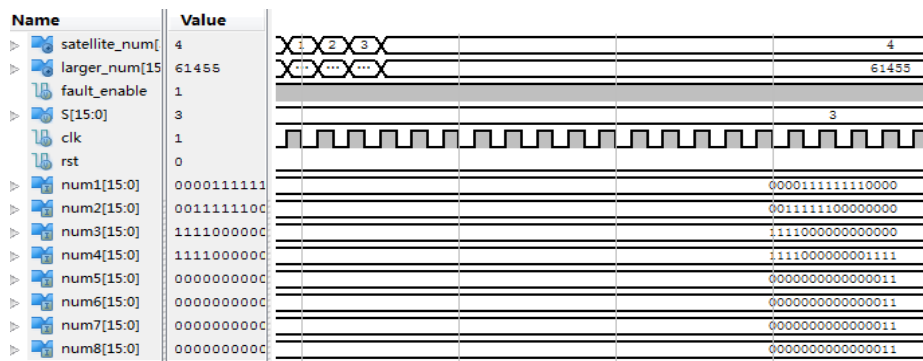


Figure 4. The simulation of the fault isolation module

As illustrated in Figure 4,  $S$  is the input of cumulative LLR function. It can be shown as followed:

$$S_j^k(q) = \sum_{i=j}^k \ln \frac{\frac{1}{N} \sum_{i=1}^N w_i^a(i)}{\frac{1}{N} \sum_{i=1}^N w_i^{main}(i)} \tag{10}$$

Where, a new data would be imported in per clock cycle. In equation (10),  $w_i^a$  is the weight of the auxiliaries particle filter, and  $w_i^{main}$  is the weight of the main particle filter,  $N$  is the number of particles. The satellite\_num is the port to output the number of the fault satellite. The larger\_num is the port to output the maximum value of the cumulative LLR function, which is proportional to the number of the fault satellite. num1, num2, ..., num8 are the cumulative LLR function of eight auxiliary PFs respectively, the rst is the reset signal and the clk is the clock signal. As is shown in Figure 4, this module is effective and can work steadily, and the output of the fault\_enable signal is equal to 1, which means the fault has been detected, and the number of the fault satellite is 4, which should be isolated during the following navigation solution.

### 4.4. The Resampling Module

In the particle filter algorithm, the variance of the importance weights will increase after a few iterations. However, the weight of most particles is getting smaller and smaller. This degeneracy means that updating particles whose are approximately to  $p(x_k | Y_{1:k})$  is almost 0 cost a lot of computational effort. Only a few of particles' weight is extremely large.

The purpose of resampling is to optimize the particles with their weight. It is an effective way to decrease the invalid samples and increase the valid particles by abandoning the small

weight particles and keeping the large weight ones. In this algorithm, the system resampling method is used. The number of the resampling particles is  $N$ , and the algorithm includes two cycles, the inner loop and the outer loop, both cycles' number are  $N$ . At the beginning of resampling, it will choose a random number  $g \in (0, 1)$  from the random noise generator, and make the summation of weights, the initialization of  $Sum$  is equal to zero. And then, it will enter the inner loop. The result of each inner cycle is that the corresponding summation of particle weight will accumulate. The value of  $Sum$  is compared with  $g$  in every inner loop. If  $Sum < g$ , it shows that the weight of current particle is small, and the particle should be abandoned. After then, according to the iteration times of inner loop, it should determine whether to continue staying in the inner loop or to be in next outer loop by comparing  $i$  with  $N$ . If  $Sum \geq g$ , it indicates that the weight of current particle is large, and the particle should be taken out. After then, according to the iteration times of outer loop, it should determine whether to be in next cycle or to complete the system resampling by comparing  $j$  with  $N$ . The particles after resampling should be stored and the weight of all stored particles is  $1/N$ . The simulation result of this module can be shown as follows in Figure 5.

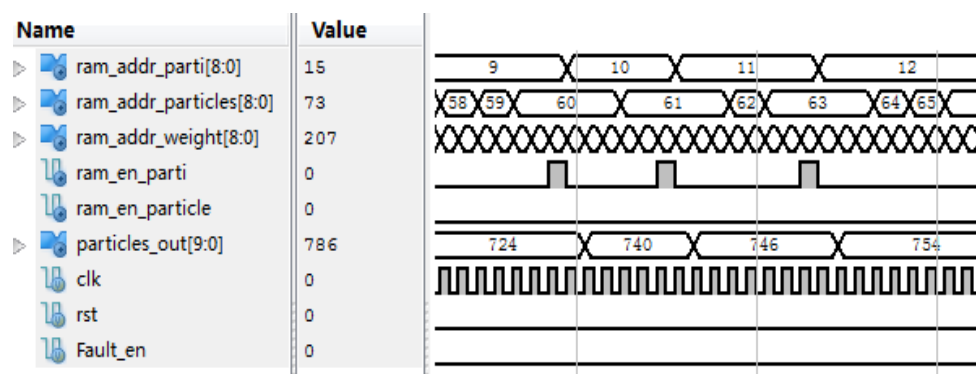


Figure 5. The simulation result of the resampling module

In the simulation result, the signal of `fault_en` is the input port of enable signal. The signal of `particles_out` is the output of the particles being resampled, the signal of `ram_en_parti` is the enable signal of RAM4 module to store the particles from the signal port of `particles_out`, and the `ram_addr_parti` is the address bus of RAM4 module, the `ram_en_particle` is the enable signal of RAM1 module that stores the particles to be resampled, and also the `ram_addr_particles` is the address bus of RAM1 module, the `ram_addr_weight` is the address bus of RAM2 module that stores the weight that corresponds the particles in RAM1 module. The resampling particles from the signal port of `particles_out` enter next cycle.

## 5. Conclusion

The RAIM algorithm for GNSS is based on PF, and the fault detection is accomplished by the log-likelihood ratio test. In addition, the paper implements some modules of the proposed RAIM algorithm by FPGA, and the main modules of the fault detection, the fault isolation and the resampling are simulated and implemented. Then, the proposed algorithm implemented on FPGA is summarized as six steps including generating the random noise, calculating the particle state, predicting the pseudorange, calculating the weight, updating the particles, Detect and isolate faults. The simulation results demonstrate that the satellite failure of GNSS is successfully detected and isolated. The proposed method has good reference value to the study BeiDou satellite navigation RAIM and improve the positioning reliability of BeiDou receiver. The RAIM algorithm implemented on FPGA for fault detection and isolation will be optimized to improve the computation efficiency of future work.

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