

Investigation Study of Three-Level Cascaded H-bridge Multilevel Inverter

Mohd Ruddin Ab Ghani^{1*}, Nabil Farah², Jurifa Lazi³, M.R.Tamjis⁴, Md Nazri Othman⁵,
Nur Huda Mohd Amin⁶, Syariffah Othman⁷, Zanariah Jano⁸, Tole Sutikno⁹

^{1,2,3,4,5,6,7}Faculty of Electrical Engineering (FKE),

⁸Centre for Languages and Human Development

^{1,2,3,4,5,6,7,8}Universiti Teknikal Malaysia Melaka, Hang Tuah Jaya, 76100 Durian Tunggal, Melaka, Malaysia.

⁹Department of Electrical Engineering, Faculty of Industrial Technology, Universitas Ahmad Dahlan (UAD),
Jln Prof. Dr. Soepomo, Janturan, Yogyakarta 55164, Indonesia

*Corresponding author, email: dpdruddin@utem.edu.my

Abstract

This paper analyzed three-level Cascaded H-bridge Multilevel Inverter (CHMLI) utilizing two modulation techniques namely Sinusoidal Pulse Width Modulation (SPWM) and Space Vector Pulse Width Modulation (SVPWM). The performance and the output of CHMLI in terms of Total Harmonic Distortion (THD) % and circuits complexity were compared. The simulations models were constructed using MATLAB/SIMULINK. The results showed the CHMLI produced the lowest THD contents and utilized fewer components. Moreover, the SVPWM produced less THD than SPWM.

Keywords: CHMLI, cascaded, MATLAB/SIMULINK, SPWM, SVPWM, THD, inverter

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1. Introduction

In the past few years, numerous research and experiments have been conducted in power electronic field in order to obtain renewable energy resources that have less impact on environment to replace the common widely used fossil-based resources which produce harmful effects to the environment and the planet [1, 2]. Most existing renewable energy resources are Direct current (DC) in nature such as solar energy and wind energy. These DC energies often require conversion to Alternative current (AC) in order to be used in daily life applications which are AC energy-based. An inverter is a device that is able to convert the DC energy into AC energy by utilizing some power electronic components [3]. However, in real life, most inverters are not capable of handling high power applications because they are mainly designed for low power applications. Hence, DC energy should be produced from renewable resources to handle high power applications. A multilevel inverter which is capable of handling small and high power application with less harmonic contents in its output should be designed [4].

In the recent few decades, a multilevel inverter has been the main focus for most researchers in the power electronic field due to its ability to deal with medium and high power application besides various advantages it offers when comparing it to the conventional two level inverter operating at the same rating. The multilevel inverter produces less harmonic contents in its output voltage and current. In addition, the power switches in multilevel inverter experience low voltage stress and low electromagnetic interferences (EMI) [4].

In this paper, two modulation techniques were used. The first technique was the Sinusoidal Pulse Width Modulation (SPWM) which utilized the idea of comparing triangular waves with sinusoidal signal to produce modulation pulse to be applied to trigger the inverter switches. The SPWM technique is the easiest and simplest modulation technique to implement with constant switching frequency [5]. The second modulation technique was the Space Vector Pulse width Modulation (SVPWM) which gave advantages over SPWM in terms of Total Harmonic Distortion (THD) contents and switching losses. However, the complexity of circuit design was much more complicated than SPWM. The idea behind SVPWM was to create a rotating space vector to be used for various applications. One method to be used in the inverter was the switching times [6].

The concept behind multilevel inverter is that it uses numerous combinations of power electronic switches to produce staircase waveform where as much as the level increases the output waveform become almost sinusoidal with low harmonic in it is output waveform [7]. Multilevel inverter topologies can be arranged in many different combinations, among the popular multilevel inverter topologies are Diode Clamped Multilevel Inverter (DCMLI), Flying Capacitor Multilevel Inverter (FCMLI) and Cascaded H-bridge Multilevel Inverter (CHMLI). All these topologies have their own combinations and features. The first multilevel topology is the Cascades H-bridge design as shown in Figure 1 which implements a set of H-bridge separate dc source inverter serially connected to produce an n-voltage level. This is followed by the diode clamped inverter as shown in Figure 2 which utilizes bank of series capacitor paralleled with dc source to produce an n-additional voltage sources. Another multilevel topology subsequently introduced is the flying capacitor design as shown in Figure 3 in which the capacitors are floating rather than series-connected. Moreover, there are different multilevel designs which involve parallel connection of inverter phases through inter-phase reactors [7].

At present, most researchers and manufacturers in power electronic field are interested in a multilevel inverter due to its advantageous in terms of harmonic reductions, better waveform output and better medium and high power applications handling [8].

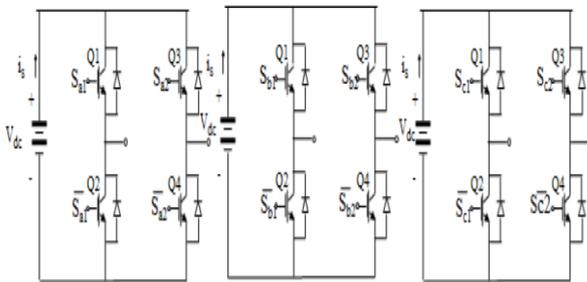


Figure 1. Three-phase 3-level CHMLI

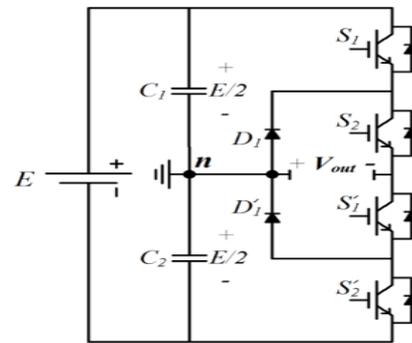


Figure 2. Three-level single phase DCMLI

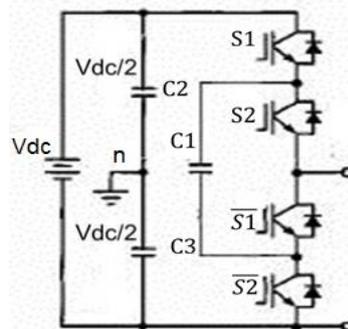


Figure 3. Three-level single phase FCMLI

This paper focused on CHMLI 3-level three-phase inverter which was constructed by connecting three H-bridge inverters in series and each bridge was fed by separate dc source. These separated dc sources feeding the H-bridge multilevel inverter could generate almost sinusoidal waveform voltage. This type of inverter could produce 3 level voltages (i.e. for 3-level H-bridge inverter could generate three different voltage outputs, $+v_{dc}$, 0, and $-v_{dc}$). Hence, the output voltage of a 3-level H-bridge 3-level inverter is the sum of all the individual inverter outputs [9]. Three levels Cascaded H-bridge Multilevel Inverter (CHMLI) was chosen in this study to demonstrate the simplicity of the circuit design and the advantageous features it offers

(Figure 4). Different modulation techniques and the results of conventional two-level inverter and other multilevel topology (DCMLI, FCMLI) are presented [10].

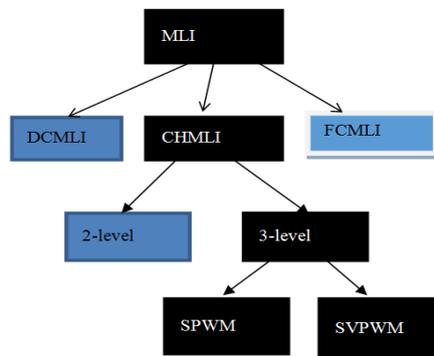


Figure 4. Block Diagram of the Research

2. Basic Principle Cascaded H-Bridge Multilevel Inverter

The cascade H-bridge multilevel inverter consisted of a number of single full bridge inverter units. Each bridge was fed by separate dc source namely battery, PV cell or any kind of dc supply. The output of each bridge could be summed up to generate almost sinusoidal output voltage waveform for nth level of CHMI each full bridge inverter unit forming the CHMI with separate dc. Four semiconductor switches are able to produce three different voltage levels namely +vdc, 0 and -vdc depending on the switching state. Each of the switching always conducts for 180 degree or half-cycle regardless of the pulse width of the quasi-square wave so that this method will result in the equalization of the current stress in each of the components [7].

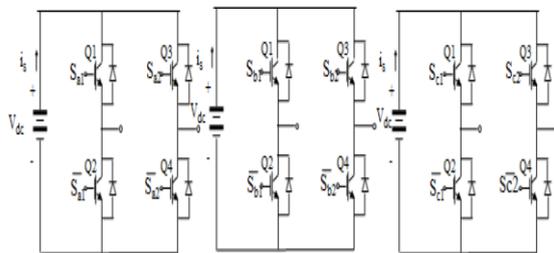


Figure 5. Three level CHMLI

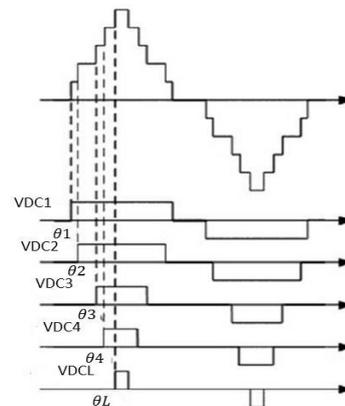


Figure 6. Staircase voltage waveform for Single-phase multilevel inverter [11]

Figure 5 shows a three-level of CHMI. Each H-bridge was activated at certain amount of time at different start up angle and because each bridge was fed by separate dc source, the output of all the bridge which formed the CHMI output would be the sum of the separated dc sources for three phase nth level of CHMI inverter. An output equation used is as follows:

$$V_{an} = V_{a1} + V_{a2} \tag{1}$$

$$V_{bn} = V_{b1} + V_{b2} \tag{2}$$

$$V_{cn} = V_{c1} + V_{c2} \tag{3}$$

From the equations above, it can be concluded that the output voltage of cascaded H-bridge multilevel inverter was the sum of the separated dc sources across the multilevel inverter. The Fourier series of bridge multilevel voltage waveform as in Figure 6 can be expanded as shown in equation 4 [11].

$$V_{out}(\omega t) = \sum_{n=1,3,5}^{\infty} b_n \sin(n\omega t) \quad (4)$$

b_n is given by:

$$b_n = \sum_{n=1,3,5..}^{2N-1} (Vdc1 \cos(na_1) + (Vdc2 \cos(na_2) + \dots \dots + (VdcL \cos(na_{L-1}) + (VdcL \cos(na_L)) \quad (5)$$

For equal and constant source the b_n is given by:

$$b_n = \sum_{n=1,3,5..}^{2N-1} vdc(\cos(na_1) + \cos(na_2) + \dots \dots + \cos(na_{L-1}) + \cos(na_L)) \quad (6)$$

Where,

$$vdc = Vdc1 = vdc2 \dots \dots \dots = vdcL$$

L= the number of dc sources for each full bridge inverter cell

N= the number of switching angles

The total harmonic distortion (THD) is a method to calculate the total distortion in the output waveform caused by the harmonics presence in the output. A general equation of the total harmonic distortion (THD) is given as follows [2]:

$$THD = \frac{\sqrt{\sum_{n=3,5..}^{\infty} (\frac{1}{n} \sum_{k=1}^S (v_k * \cos(n\theta_k)))^2}}{\sum_{k=1}^S (v_k * \cos(n\theta_k))} \quad (7)$$

3. Modulation Techniques

In terms of the control strategy of a multilevel inverter, numerous researchers in the power electronic field have developed many modulation techniques. The two famous and simple modulation techniques are the Sinusoidal Pulse Width Modulation (SPWM) and, the Space Vector Pulse Width Modulation (SVPWM). A multilevel inverter switching signal can be generated using these two methods with less switching losses and harmonic distortion.

3.1. Sinusoidal Pulse Width Modulation (SPWM)

The CHMI was controlled by the SPWM where sinusoidal wave was compared with square waves to generate the switching signal that would trigger the semiconductor switches in time sequence considering the phase between the phases shift three phase inverter legs. This method used N-1 level carrier signals to generate the N-level inverter output voltage. In multilevel inverter, the frequency modulation index, m_f and the amplitude modulation index, m_i is defined as follows [12, 13]:

$$m_f = \frac{f_c}{f_m} \quad (8)$$

$$m_i = \frac{A_m}{A_c} \quad (9)$$

Where f_c = carrier signal frequency, f_m = reference signal frequency,
 A_c = carrier signal amplitude, A_m = reference signal amplitude.

This paper was to analyze and compare three-level inverter. To generate the switching pulses of 3-level inverter utilizing sinusoidal pulse width modulation, two carrier signals were compared with one reference sine wave where the amplitude of the carrier signal was divided

into two regions to fit the reference sine wave amplitude. Figure 7 and 8 show the SPWM carriers signal compared with reference sinusoidal signal for 2-level and 3-level inverter.

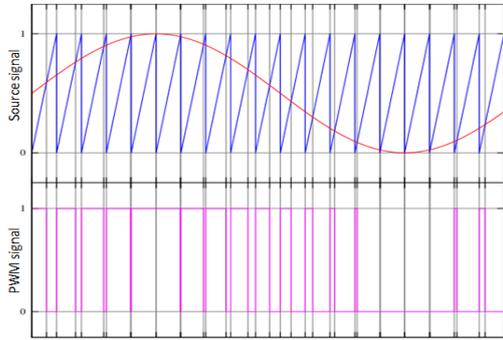


Figure 7. The SPWM carriers signals of 2-level inverter

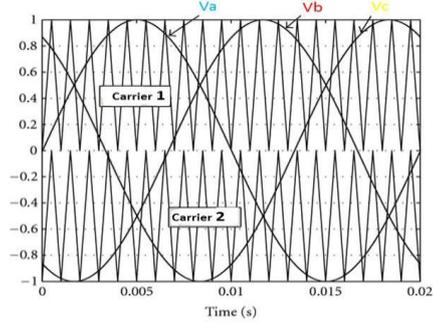


Figure 8. The SPWM carriers signals of 3-level inverter

3.2. Space Vector Pulse Width Modulation (SVPWM)

Space Vector Modulation (SVM) is an algorithm for the control of pulse width modulation (PWM). The idea behind SVPWM is to create a rotating space vector that will be used for various applications. One method to be used in inverter was the switching times.

The circuit in Figure 9 demonstrates the foundation of a two-level voltage source converter. It had six switches (sw1-sw6) and each was represented by an IGBT switching device. A, B and C represented the output for the phase shifted sinusoidal signals. Depending on the switching combination, the inverter would produce different outputs, creating a two-level signal. The biggest difference from other PWM methods was that the SVPWM used a vector as a reference. This offers a better overview of the system [14].

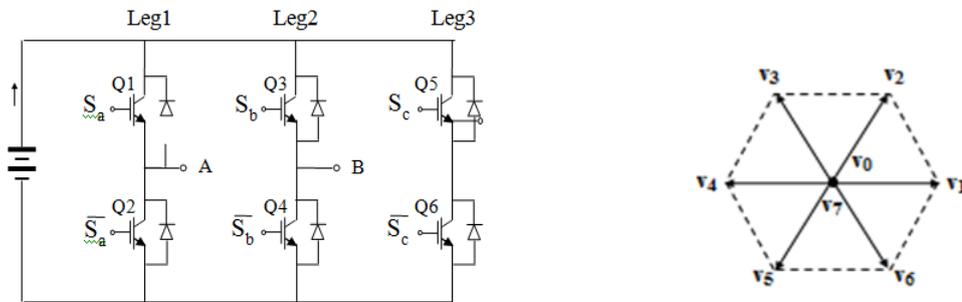


Figure 9. The two level voltage source inverter with its voltage vectors

3.2.1. References Vector

The reference vector was represented in a $\alpha\beta$ -plane. A two-dimensional plane was transformed from a three-dimensional plane containing the vectors of the three phases. The ON or OFF switch was determined by the location of the reference vector on this $\alpha\beta$ -plane (Figure 10).

The space vector of a three-level inverter is shown in Figure 11. It was composed of six space vector diagrams of two-level inverter. Each space vector of two-level inverter was centered at the six apexes of the inner hexagon. Thus, if each of the six small hexagons was moved toward the center of the inner hexagon by $V_{dc}/3$ according to their location, the space vector diagram of a three-level inverter was simplified to that of two-level inverter.



Figure 10. The references vectors for sector 1 and the reference vector in all sector

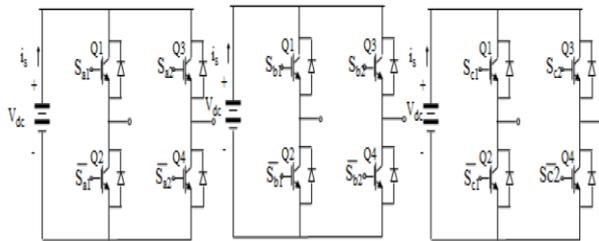


Figure 11. The three-level inverter

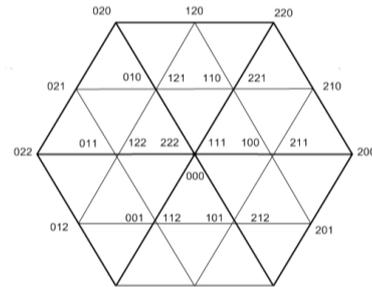


Figure 12. The 3-level inverter voltage vector

3.2.2. Derivation of Reference Voltage

SVPWM method of three-level inverter is similar to that of Conventional two-level SVPWM in principle. Hence, various techniques which are used in two-level SVPWM, can be adopted to this method. Figure 12 shows the space vector simplification of three-level inverter [15].

The space vector of three-level inverter can be simplified to that of two-level inverter. The number in Figure 13, represented as s, is the index that denotes the six small hexagons, constituting the three-level space vector diagram. Regions exist which are shared by adjacent small hexagons in the three-level space vector diagram [15].

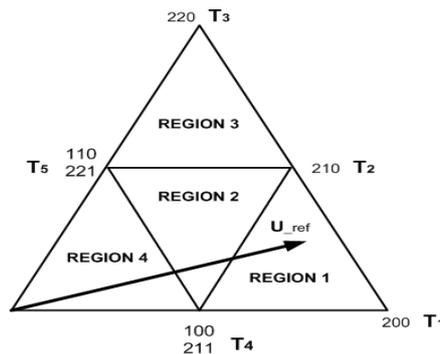


Figure 13. Dividing sector into four triangular regions

3.2.3. Total Harmonic Distortion (THD)

The basic definition of total harmonic distortion is the summation of all harmonic components of the Voltage or current waveform compared against the fundamental component of the voltage or current wave [16]. In other words, harmonic distortion is the noise or distortion

presented in the output voltage or current waveform which causes the waveform to be distorted and does not produce a pure sinusoidal signal. The harmonic distortion is produced due to the components of the inverter and control strategy used to trigger the inverter semiconductor switches. The harmonics distortion, hence, needs to be investigated and analyzed in order to propose a method to reduce these distortions.

$$\%THD = \frac{\sqrt{(v_2+v_3+v_4+\dots+v_n)^2}}{v_1} \times 100 \tag{10}$$

Where:

- THD= Total harmonic distortion
- v_1 = Fundamental Voltage magnitude
- v_2 = Magnitude of 2nd Harmonic
- v_3 = Magnitude of 3rd Harmonic
- v_n = Magnitude of nth Harmonic

In the case of multilevel inverter which produces stepped waveform, another accurate formula to calculate the THD is proposed which utilizes the switching angle of the wave form as shown in equation 11.

$$THD = \frac{\sqrt{\sum_{n=2}^{\infty} H(n)^2}}{H_1} \tag{11}$$

Where:

- H_1 is the amplitudes of the fundamental component, whose frequency is ω_0
- And $H(n)$ is the amplitudes of the nth harmonics at frequency $n\omega_0$

4. Simulation Results

To verify the theoretical analysis, three-level CHMLI was constructed using SPWM and SVPWM. A conventional two-level inverter and two other topologies of 3-level inverter (DCMLI, FCMLI) were also constructed and presented along with their simulation results for the purpose of comparison and illustration of preference and superiority of CHMLI among other topologies as well.

Figure 14 and 15 show the conventional two level inverter circuit controlled by SPWM and SVPWM.

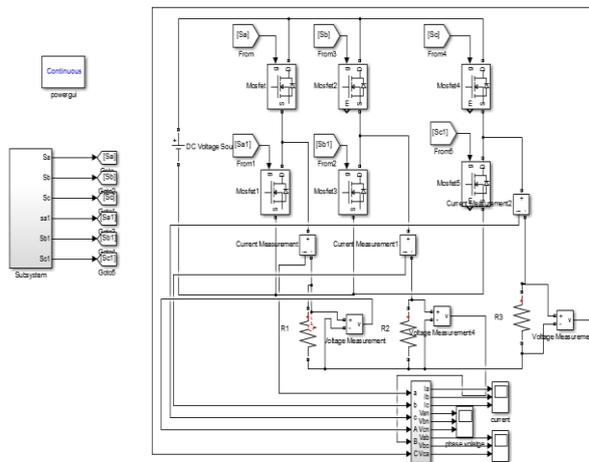


Figure 14. The two level inverter circuit and its gating signal (SPWM)

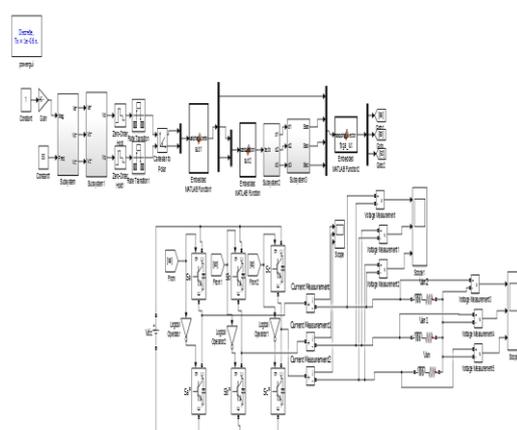


Figure 15. The two level inverter circuit and its gating signal (SVPWM)

Figure 16 and 17 show the three-level inverter controlled with SPWM and SVPWM along with the modulation circuits. Figures 18 and 19 show the three levels inverter DCMLI and FLCMLI.

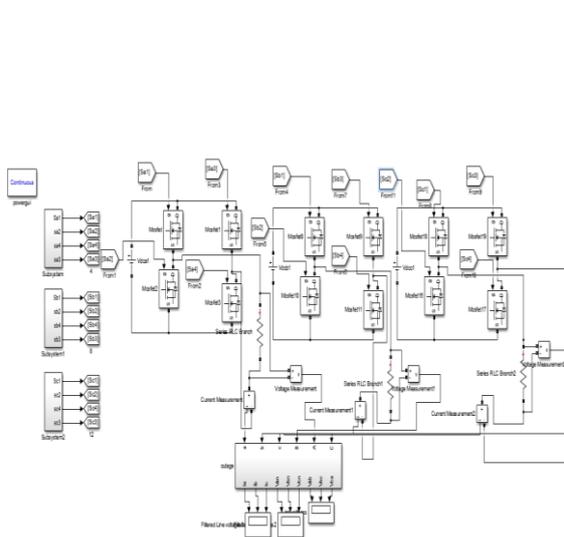


Figure 16. Three level cascaded h-bridge multilevel inverter with its control signal (SPWM)

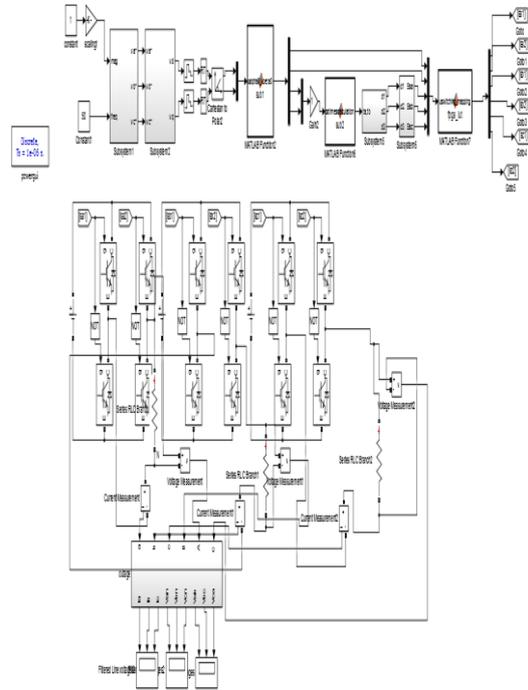


Figure 17. Three level inverter using SVPWM

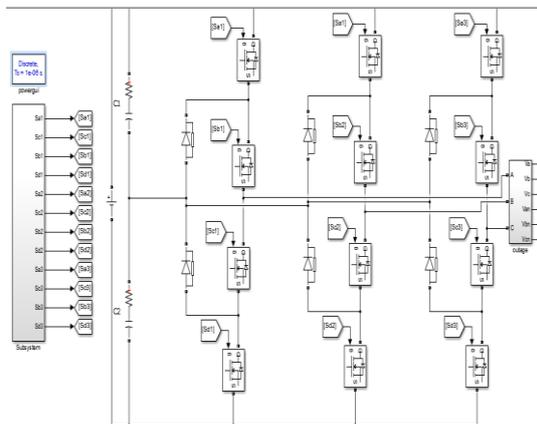


Figure 18. Three level diode clamped multilevel inverter with its control circuit

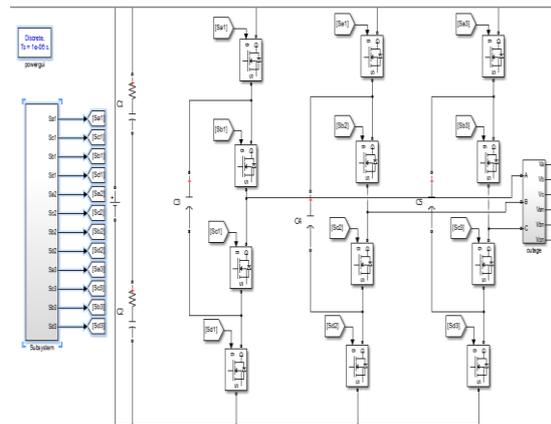


Figure 19. The three level flying capacitor with its control circuit

4.1. Cascaded H-bridge Multilevel Inverter

Initially, the two level inverter results were presented using SPWM followed by the results of SVPWM. Figure 20 shows the comparison of carrier signal with sine wave signal to generate the pulse for two-level inverter. While Figure 21 shows the line voltage of two-level inverter. Figure 22 shows the THD analysis of two level inverter output line voltage using SPWM.

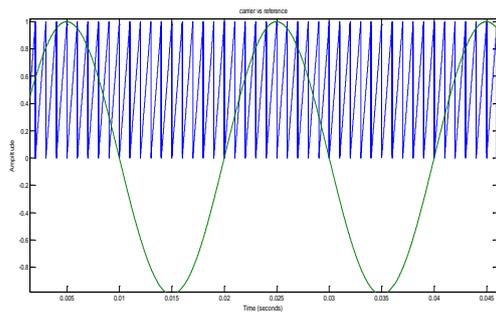


Figure 20. Comparison of carrier with reference sine wave for two-level inverter

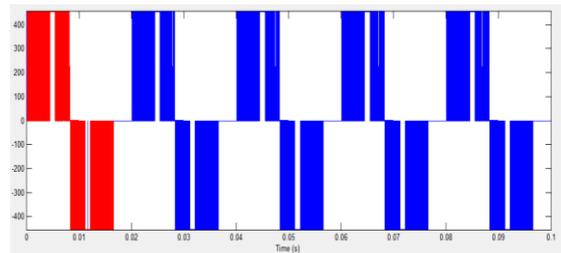


Figure 21. Output line voltage of two level inverter using SPWM

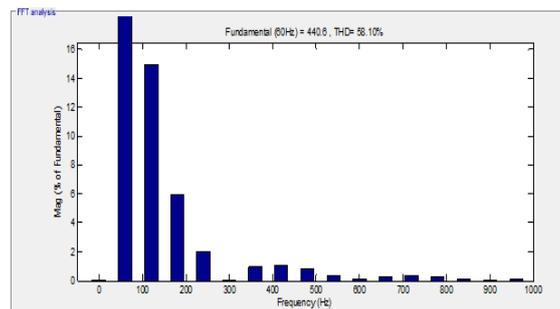


Figure 22. THD of line voltage of two-level inverter with SPWM

While Figure 23 shows the output line voltage of two-level inverter using SVPWM. Figure 24 shows the THD analysis of line voltage of two-level inverter with SVPWM.

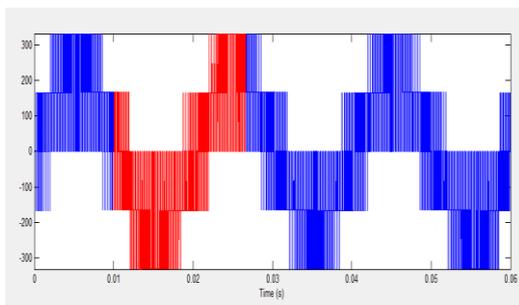


Figure 23. Output of line voltage of two-level inverter using SVPWM

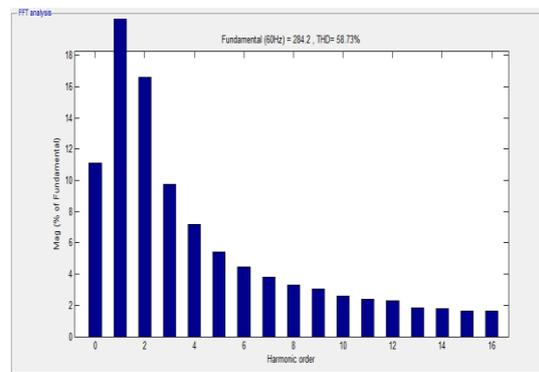


Figure 24. THD of line voltage of 2 level inverter using SVPWM

For three-level inverter, Figure 25 shows a comparison between carrier signals and references signal for three-level inverter. Figure 26 shows the output line voltage of three level inverter using SPWM and Figure 27 shows the THD analysis of three level inverter using SPWM as well.

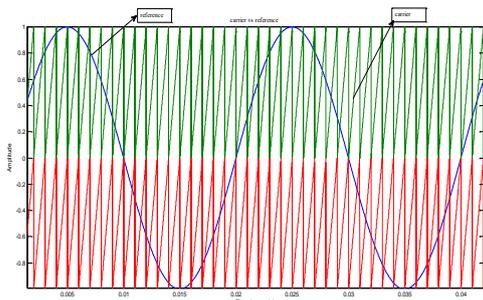


Figure 25. Compression of carrier signal against reference signal

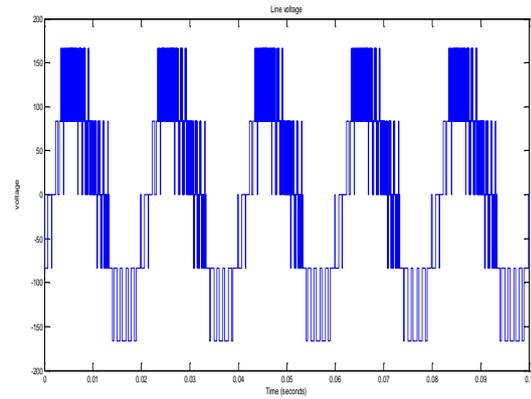


Figure 26. Output current of three-level inverter using SPWM

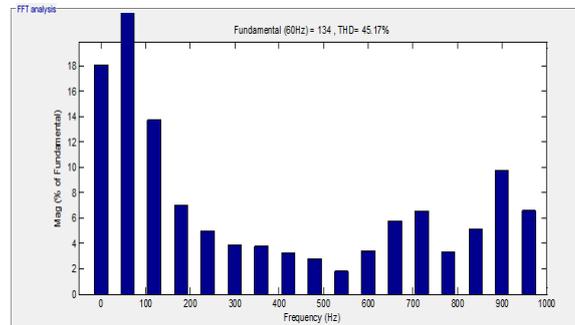


Figure 27. THD of three level inverter output current using SPWM

In addition, the three-level inverter has been modeled using SVPWM. Figure 28 shows the output line voltage of three-level inverter using SVPWM and Figure 29 shows the THD analysis of three-level inverter with SVPWM as well.

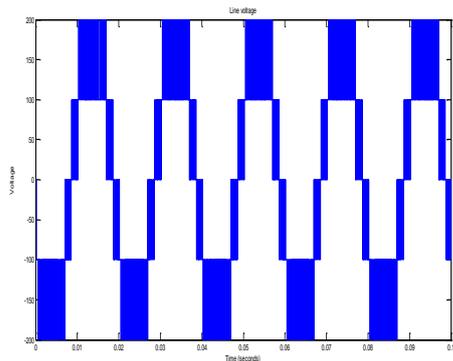


Figure 28. The output of line voltage of three-level inverter using SVPWM

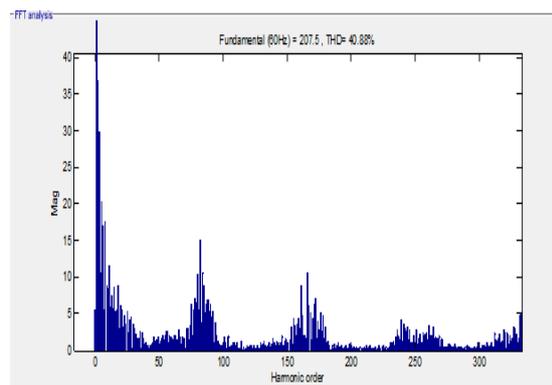


Figure 29. LINE THD of three level inverter using SVPWM

Moreover, for the aim of comparison, the output of DCMLI and FCMLI are presented here. Figure 30 shows the output line voltage of three-level DCMLI and Figure 31 shows the THD analysis of three-level DCMLI.

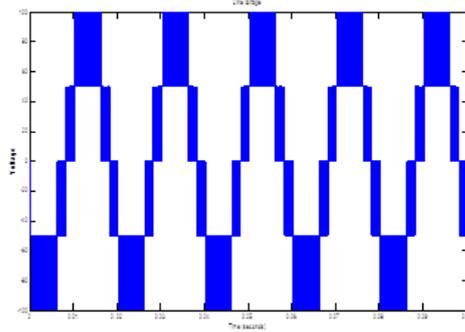


Figure 30. Output line voltage of three-levels DCMLI using SPWM

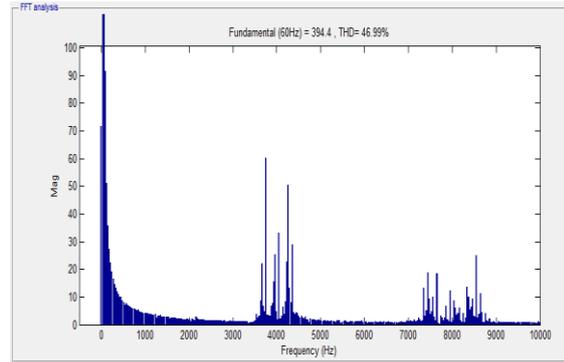


Figure 31. THD of line voltage of three-level DCMLI

5. Results Analysis

Table 1 shows the tabulated value of inverter output Line voltage THD with respect to the number of output levels of CHMLI (Cascaded H-bridge Multilevel Inverter).

Table 1. The tabulated value of inverter output voltage THD with parameters variation

| Number of level | SPWM | SVPWM |
|-----------------|--------|--------|
| 2 | 58.10% | 56.49% |
| 3 | 45.17% | 40.88% |

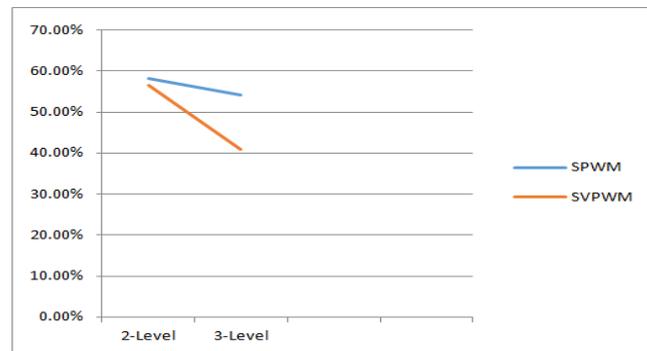


Figure 32. THD Analysis

The THD value is tabulated in Table 1 and the graph in Figure 33. The THD of the inverter was reduced if the inverter was controlled using space vector pulse width modulation. A reduction from 45.17% when using sinusoidal pulse width modulation (SPWM) to 40.88% when using the SVPWM was observed, indicating that the Space vector modulation technique is the best solution in terms of output voltage, harmonic losses and number of switching per cycle.

As the aim of this paper was to propose different multilevel inverter topologies and compare them in terms of different aspects, Table 2 shows the comparison among the three MLI topologies.

Table 2. Comparisons between MLI topologies

| Inverter type | No.level | Carrier frequency | THD% | Modulation techniques |
|---------------|----------|-------------------|--------|-----------------------|
| CHMLI | 3 | 10000 | 45.17% | SPWM |
| DCMLI | 3 | 10000 | 46.99% | SPWM |
| FCMLI | 3 | 10000 | 46.18% | SPWM |

Figure 33 shows the THD % graph for three different multilevel topologies. Hence, the CHMLI has the lowest THD% among the topologies. Table 3 shows the comparison between MLI topologies in terms of components used for three-level inverter.

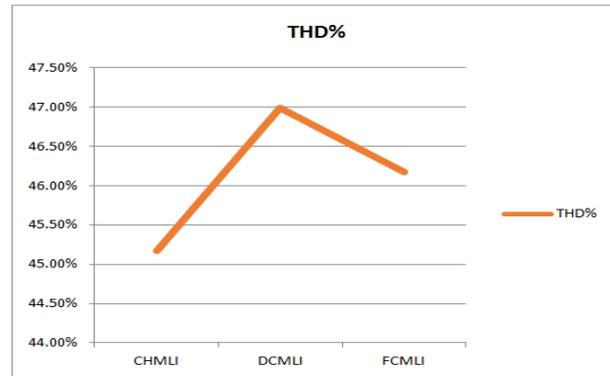


Figure 33. THD Analysis Graph

Table 3. Number of Components used in Each MLI Topology

| Inverter type | Number of switches | Numbers capacitors | Number of diodes | Total of components |
|---------------|--------------------|--------------------|------------------|---------------------|
| CHMLI | 12 | 0 | 0 | 12 |
| DCMLI | 12 | 2 | 6 | 20 |
| FCMLI | 12 | 12 | 0 | 24 |

Based on the information tabulated above and the THD curve, the CHMLI has the best THD% compared to other topologies. Besides, it utilizes the fewest semiconductor devices where it neither requires any clamping diode nor balancing capacitor. In addition, the CHMLI is the easiest topology in terms of circuit complexity especially when implementing higher inverter levels.

6. Conclusion

This present study has investigated three-level inverter, focusing mainly on Cascaded H-bridge Multilevel Inverter (CHMLI) by utilizing two modulation techniques namely Sinusoidal Pulse Width Modulation (SPWM) and Space Vector Pulse Width Modulation (SVPWM). The paper compares the three-level CHMLI against conventional two-level inverter in terms of Total Harmonics Distortion (THD) with respect to different modulation techniques. Moreover, other multilevel topologies like (DCMLI and FCMLI) are included as well to compare them with CHMLI in terms of THD%, number of components used and circuits complexity. Hence, the findings yield that the CHMLI produces the lowest THD contents and utilizes fewer components. Moreover, the SVPWM produces less THD than SPWM.

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